

Introduction to Causal Machine Learning

Amit Sharma

Principal Researcher

Microsoft Research

www.amitsharma.in

Twitter: [@amt_shrma](https://twitter.com/amt_shrma)

Two session series on Causal ML

- **Session 1: Intro to causal machine learning**
 - Estimating causal effect, explaining outcomes, and out-of-distribution generalization
- **Session 2: Causal machine learning in practice**
 - PyWhy/DoWhy and the promise of large language models

Session goals: Intro to causal machine learning

- What is the difference between **causal** and **predictive** machine learning (ML)?
 - **Side-goal:** Learn about causality fundamentals
- When is causal ML **useful**?
- What can you achieve with causality + ML?
 - **Looking forward:** Take **better decisions**
 - **Looking backward:** **Explain the reasons** for observed outcomes
 - **Improving ML models:** **Better generalization** of ML models

Outline

1. What is causal ML and why do we need it?

1. What can you achieve using causal ML?
2. When is it practically useful compared to predictive ML?

2. Fundamental concepts in causality

1. Interventions and counterfactuals
2. Causal graph

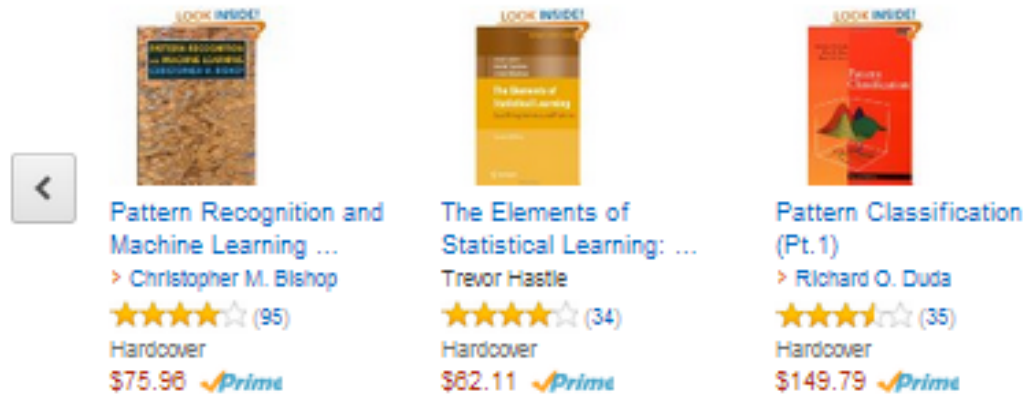
3. Three main applications

1. Choosing the “best” decision for a target outcome
2. Attributing causes for a target outcome
3. Building predictive models that generalize out-of-distribution

Section 1: What is causal ML and why do we need it?

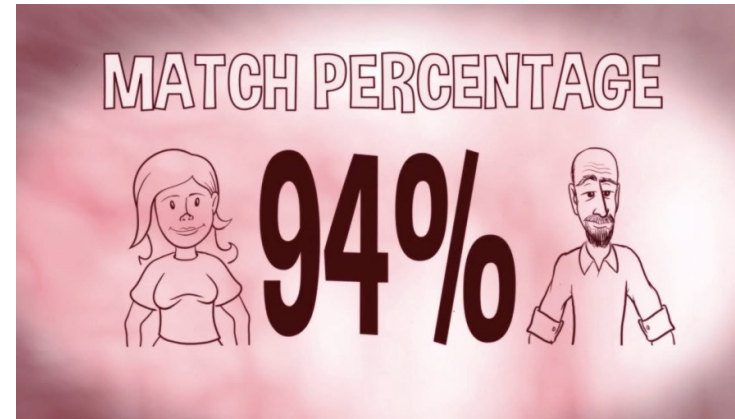
When we think of machine learning, we often think of predictions: What does the data say?

Customers Who Bought This Item Also Bought



A screenshot of an Amazon product recommendation section titled "Customers Who Bought This Item Also Bought". It features three book covers with their respective titles, authors, ratings, and prices. Each item has a "Prime" badge.

Book Title	Author	Rating	Price
Pattern Recognition and Machine Learning ...	Christopher M. Bishop	★★★★☆ (95)	\$75.96
The Elements of Statistical Learning: ...	Trevor Hastie	★★★★☆ (34)	\$62.11
Pattern Classification (Pt. 1)	Richard O. Duda	★★★★☆ (35)	\$149.79



But there's an important class of problems about **decisions: what action should I take?**



Which customers should we provide discounts to improve sales?



Which treatment will have the best improvement for a patient?



What is the best way to share an important public safety message?



Would this government regulation lead to a decrease in air pollution?

Sometimes, these problems overlap...

- Accurate prediction also means accurate decision-making.



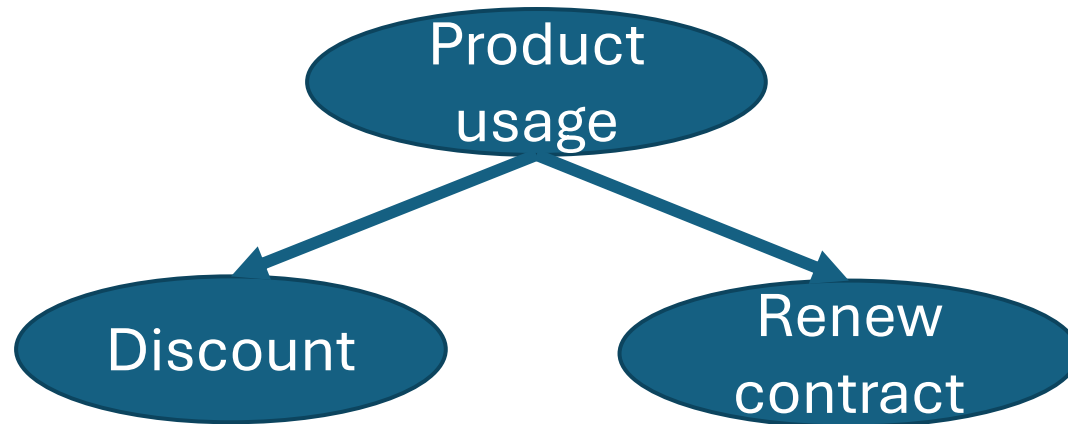
- **Prediction task:** Does the X-ray image indicate a tumor?
- **Decision task:** Should we give tumor treatment or not?

But sometimes, they do not



- **Prediction task:** Predict the customers most likely to churn out.
- **Decision task:** Who to provide discounts to?
 - Discounts may not work on people likely to churn out (low activity)
 - May be unnecessary for people with high activity.
 - **Only need to find the people in the middle**, who are undecided.

Reason: Correlation versus causation



- Today's product usage can predict tomorrow's probability of churn (not renewing contract).
- But does not tell us anything about effect of discount.
 - Effect could even be zero!

And often, decision-making requires solving a new kind of problem: **effect estimation**

- **Effect estimation:** What is the effect of an action on the outcome?



What is the best way to share an important public safety message?

Q: What is the effect of sharing medium on response rate for the safety message?



Would this government regulation lead to a decrease in air pollution?

Q: What is the effect of the regulation on air pollution?

In effect estimation, the most important task is **how to avoid being fooled by correlations**



What is the best way to share an important public safety message?

Observed data: The response rate of text messages is the highest.

Selection bias: Dataset contains mostly young people.



Would this government regulation lead to a decrease in air pollution?

Observed data: In other states, pollution decreased after the regulation.

Confounding bias: Other states differ on the kind of industries they have.

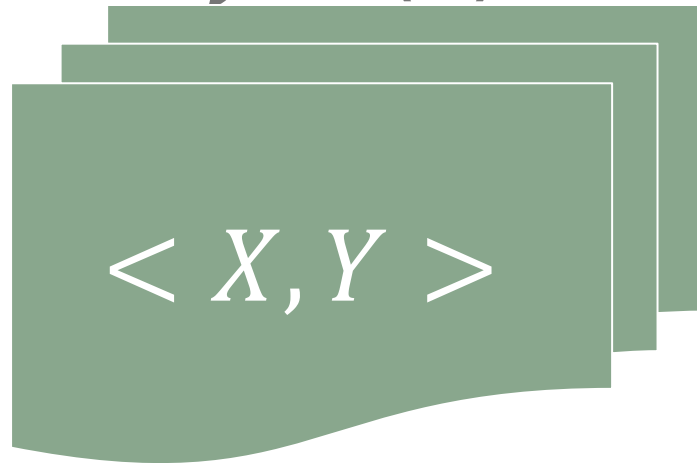
So, how to solve these problems in a systematic way?

Incorporate techniques for **learning causality** in ML models.

Causal ML is about inferring the **best actions** (and the effects of actions in general)

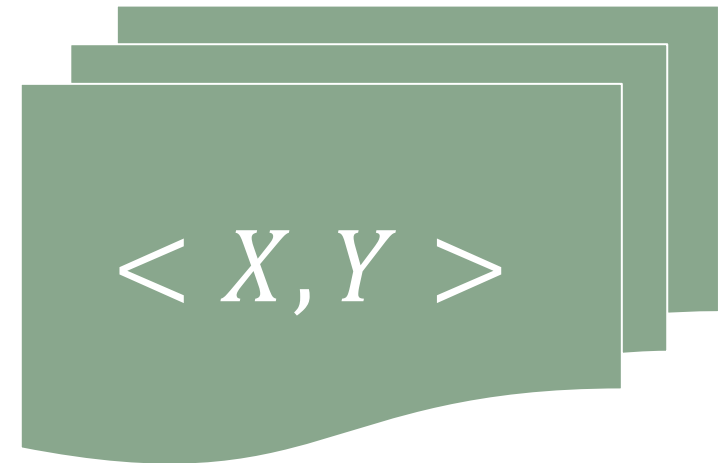
Prediction ML:

$$y = h(x) + \epsilon$$



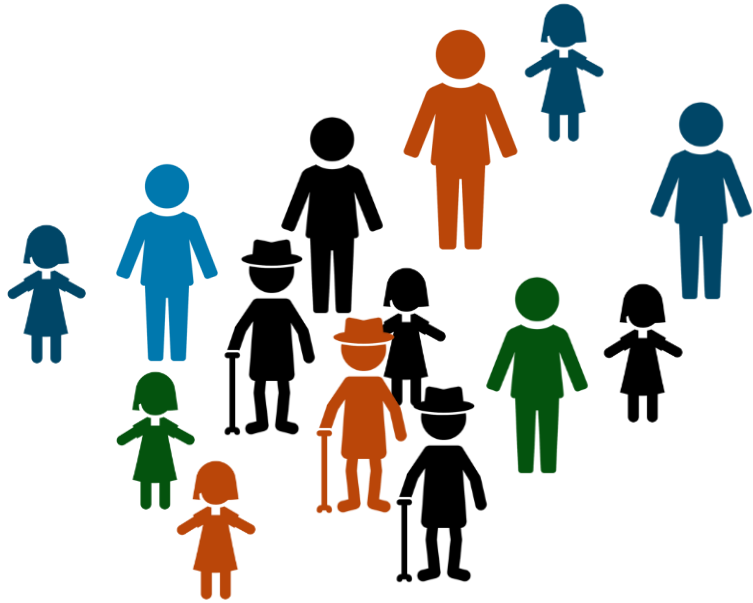
Causal ML:

$$\partial f(x, u) / \partial x$$



True:
 $y = f(x, u) + \epsilon$

Three key applications of causal ML: **Better decision-making** (what to do next?)



People who do not cycle
have high cholesterol

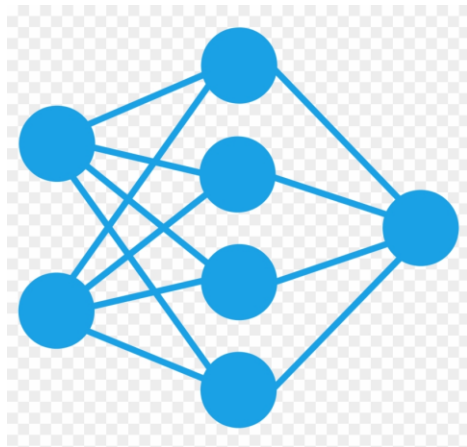


People who cycle regularly
have low cholesterol

Decision: To improve cholesterol levels of the population, should the city government invest in programs for encouraging cycling (e.g., giving free bikes)?

Three key applications of causal ML:

Root cause attribution (why did this happen?)



Predicted Class

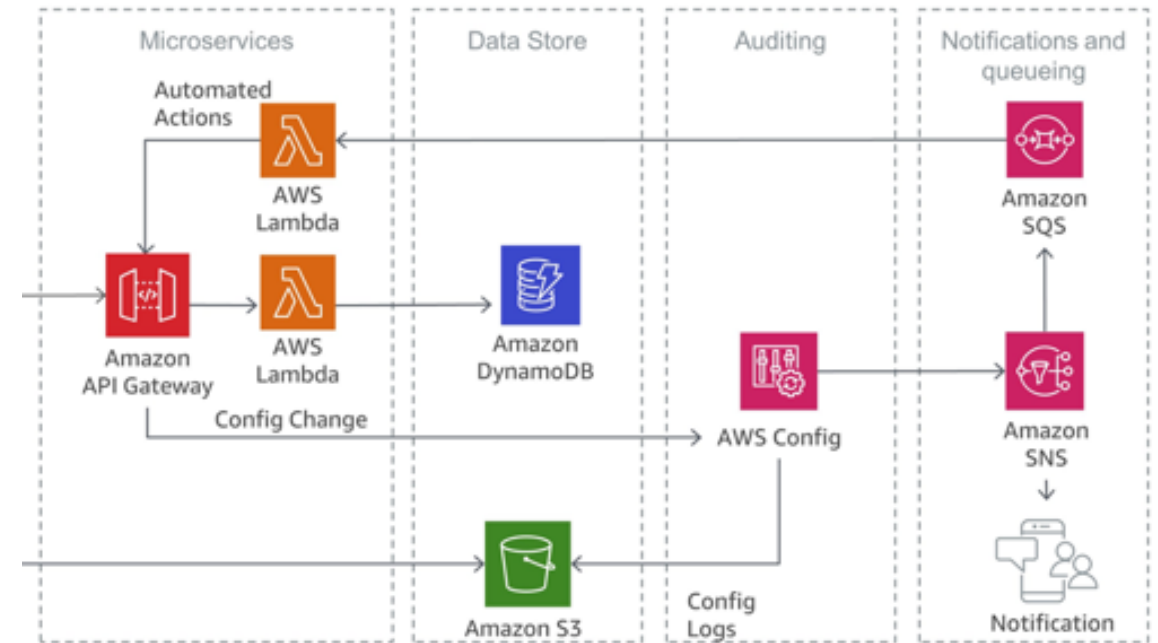
Class: 1

Class: 0

Class: 0






Class: 1

Attribution: Why did the classifier predict Class:1 for the first image?



Attribution: For a given the microservice system, why did the latency increase?

Three key applications of causal ML: **Out-of-distribution generalization**

Satellite Image (x)					
Year / Region (d)	2002 / Americas	2009 / Africa	2012 / Europe	2016 / Americas	2017 / Africa
Building / Land Type (y)	shopping mall	multi-unit residential	road bridge	recreational facility	educational institution

To summarize,

Causal ML:

Machine learning + causality

A necessary ingredient for general-purpose AI

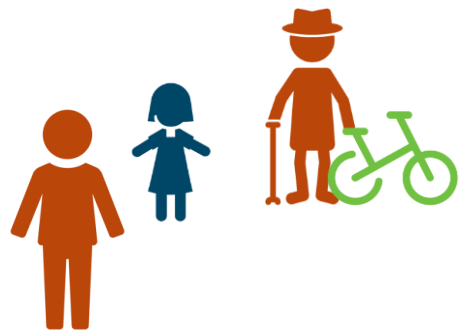
Section 2: Fundamental concepts in causality

(intervention, counterfactual, & causal graph)

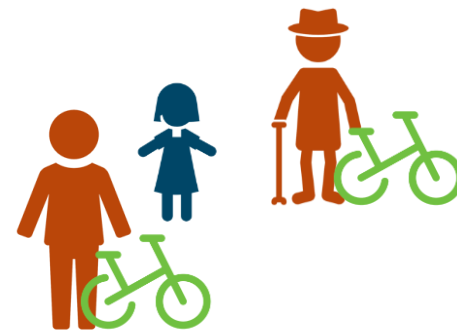
Intervention: A formal definition for taking an action

Intervention: An active action taken that changes the distribution of a variable T .

- Different from *observing* two different values of T .



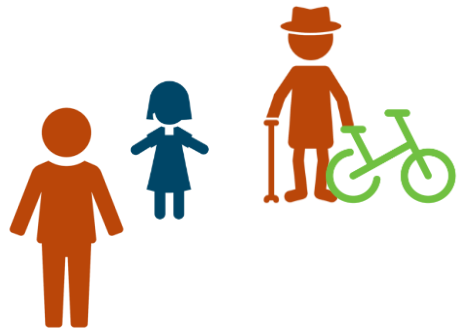
Intervention
→



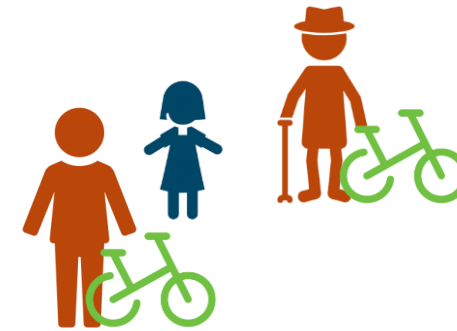
Observed data
Cycling (T)={0,0,1}

Interventional data
Cycling (T)={1,0,1}

Mathematically represented using the do-operator



Intervention



Observed data

Cycling (T)={0,0,1}

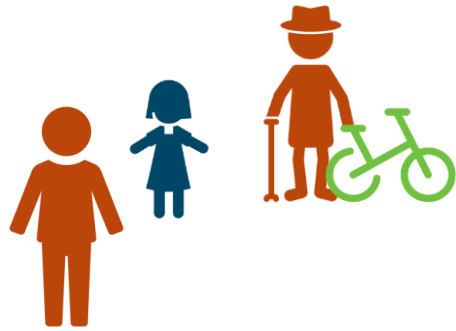
Interventional data

Cycling (T)={1,0,1}

$P(\text{Health}|\text{Cycling}, \text{Age}, \text{Color})$

$P^*(\text{Health}|\text{Cycling}, \text{Age}, \text{Color})$
 $=P(\text{Health}|\text{do}(\text{Cycling}), \text{Age}, \text{Color})$

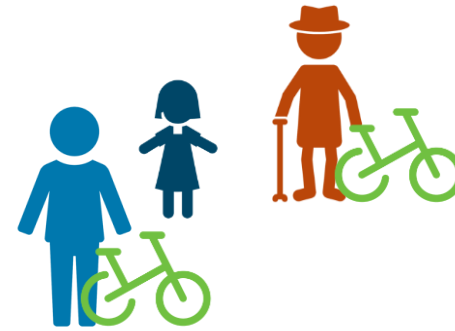
Important: A do-intervention affects only the desired variable, **keeping everything else fixed**



Observed data 1
Cycling (T)={0,0,1}

$P(\text{Health}|\text{Cycling}, \text{Age}, \text{Color})$

Not an
Intervention →

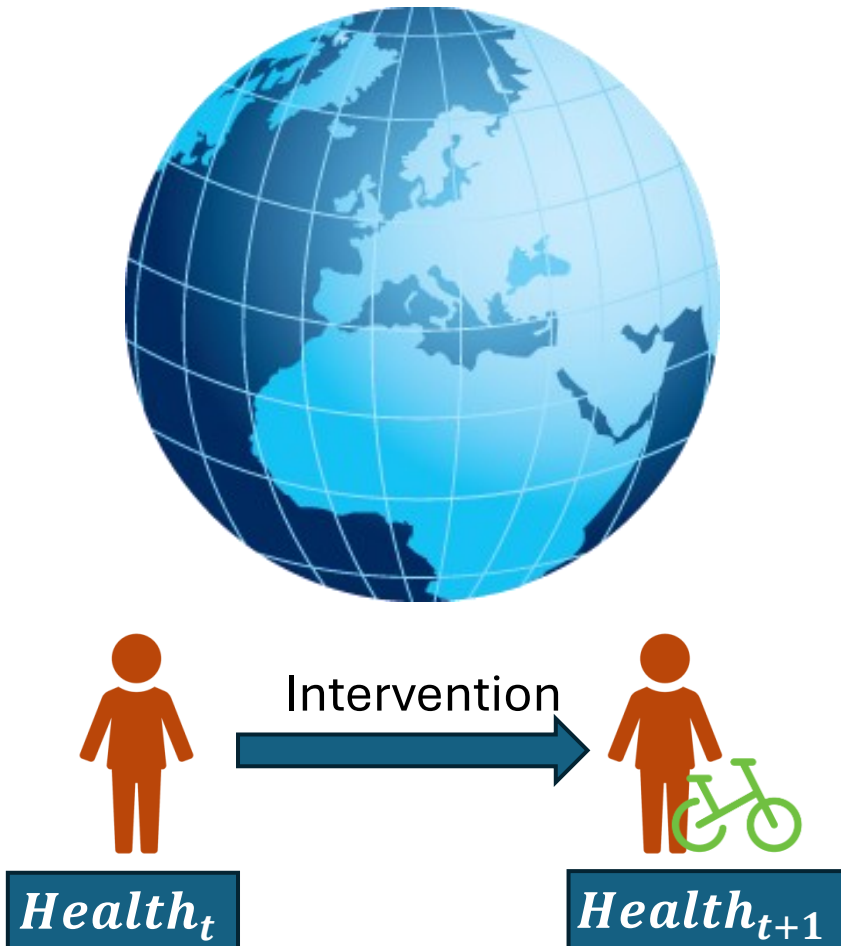


Observed data 2
Cycling (T)={1,0,1}

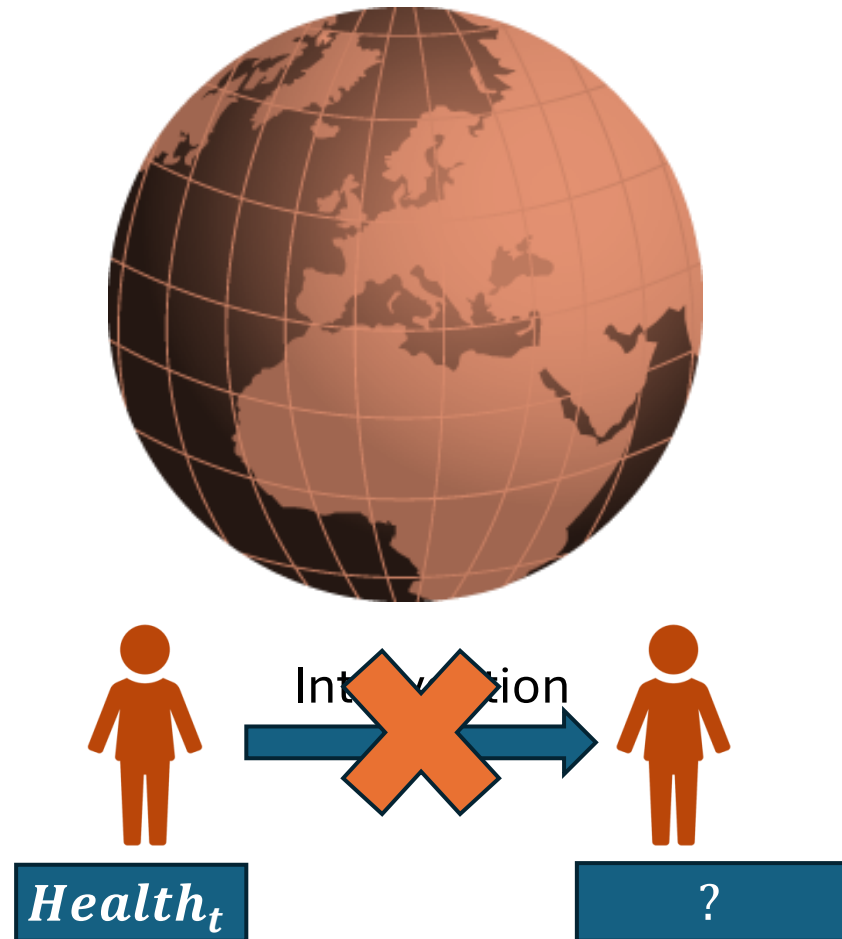
$P^*(\text{Health}|\text{Cycling}, \text{Age}, \text{Color})$
 ~~$=P(\text{Health}|\text{do}(\text{Cycling}), \text{Age}, \text{Color})$~~

Second important concept: **counterfactual** (What would have happened *if*)

Real World



Counterfactual World



Counterfactual: Complicated to express formally,
but intuitive to grasp

$$P(\text{Health}_{t+1,0} | \text{Health}_{t+1}^*, \text{Health}_t^*, \text{Cycle}_{t+1} = 1, \text{do}(\text{Cycle}_{t+1}) = 0)$$

Given that person started cycling and improved their health, **what would have happened to their health if they did not start cycling, but everything else remained the same?**

Now we are ready to define the **causal effect** of a variable

Definition: X causes Y iff
changing X leads to a change in Y,
keeping everything else constant.

The **causal effect** is the magnitude by which Y is changed by a unit change in X.

$$P(Y|do(X = 1)) - P(Y|do(X = 0))$$

Real World



Counterfactual World



As we will see, the key problem is that one of the terms is **never observed in data**

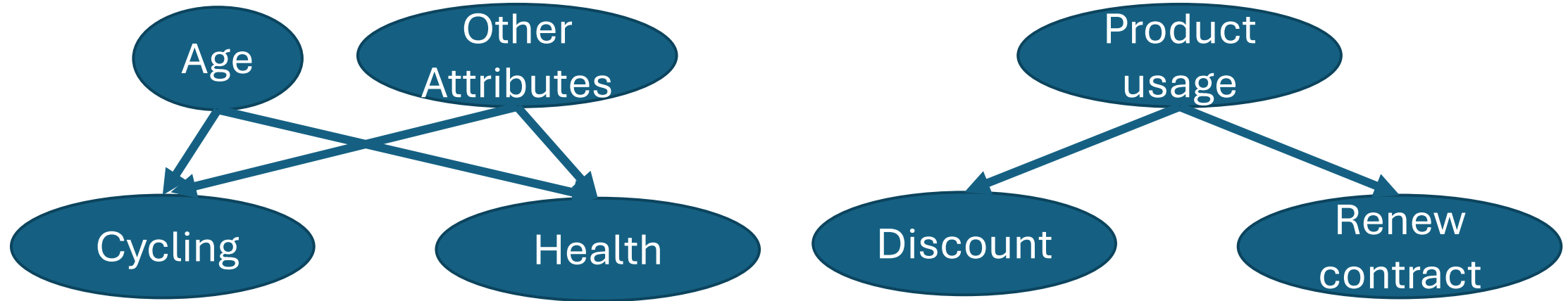
$$\begin{aligned} & P(Y|do(X = 1)) - P(Y|do(X = 0)) \\ &= P^{obs}(Y|X = 1) - P(Y|do(X = 0)) \end{aligned}$$

Predictive ML solves the problem by assuming

$$P(Y|do(X = 0)) = P^{obs}(Y|X = 0)$$

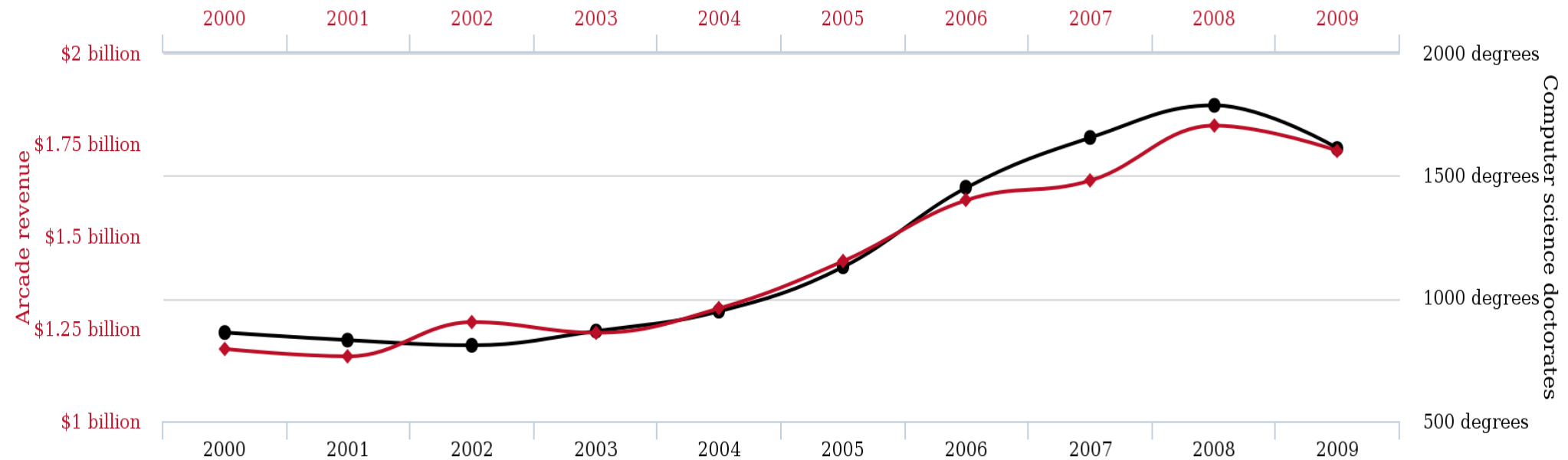
The goal of causal ML is to find a better approximation.

Final concept: **Causal graph** to encode assumptions that help estimate the unseen



- A good graph exposes the key assumptions about how different variables affect each other
 - $A \rightarrow B$ or $B \rightarrow A$?

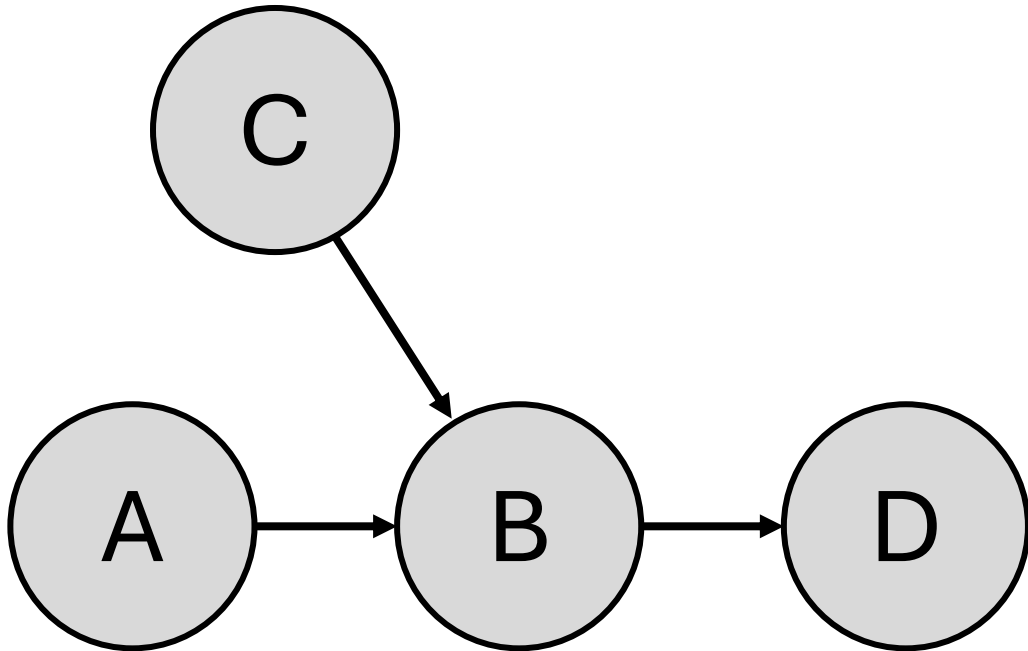
Failure case: What can happen without causal assumptions?



tylervigen.com

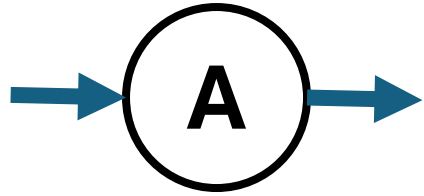
<http://www.tylervigen.com/spurious-correlations>

Interpreting a causal graph: **d-separation**

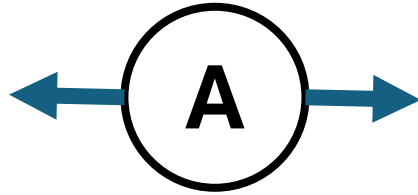


- Edges encode mechanisms
 - *direct causes*
- Graph implies conditional statistical independences
 - E.g., $A \perp\!\!\!\perp C$, $D \perp\!\!\!\perp A \mid B$, ...
 - Identified by *d-separation* rules

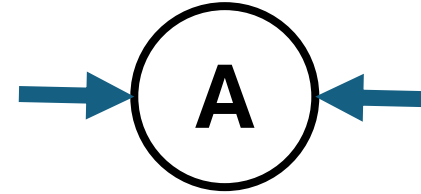
Interpreting a causal graph: **d-separation**



If conditioned on X



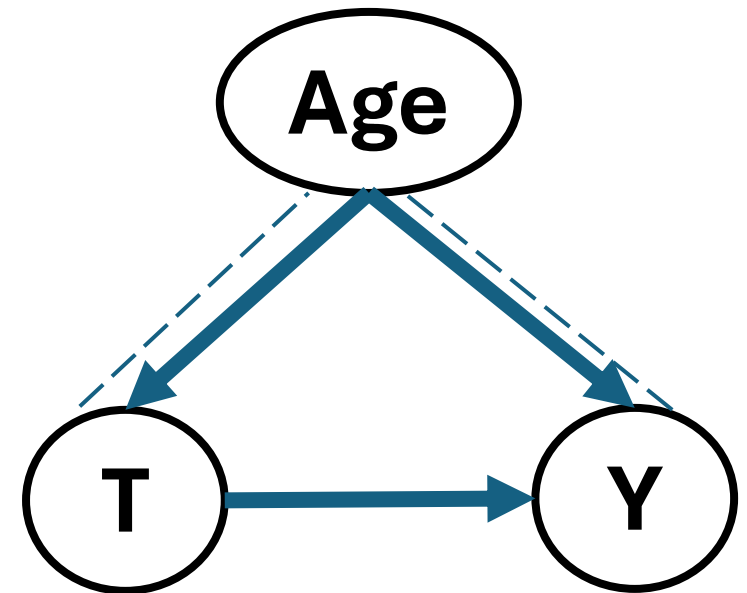
If conditioned on X



If not conditioned on X

Three kinds of node-edges

Path is “blocked” → path is d-separated



$X = \{Age\}$

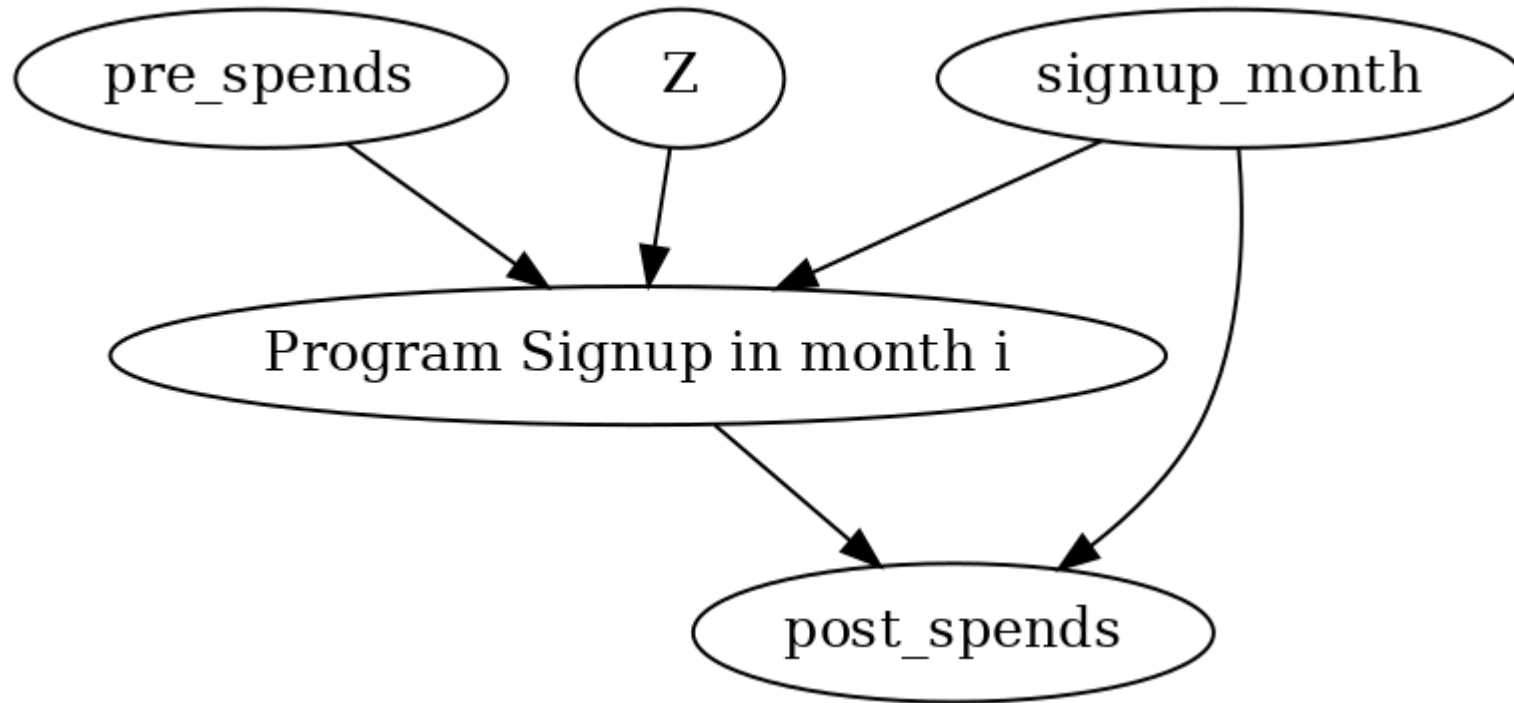
Insight: The assumptions are not the edges you create, but the edges you omit

- Assumptions are encoded by *missing edges*, and *direction* of edges
- Relationships represent stable and independent mechanisms
- It is **not always possible** to learn a graph from observational data

How to obtain a causal graph?

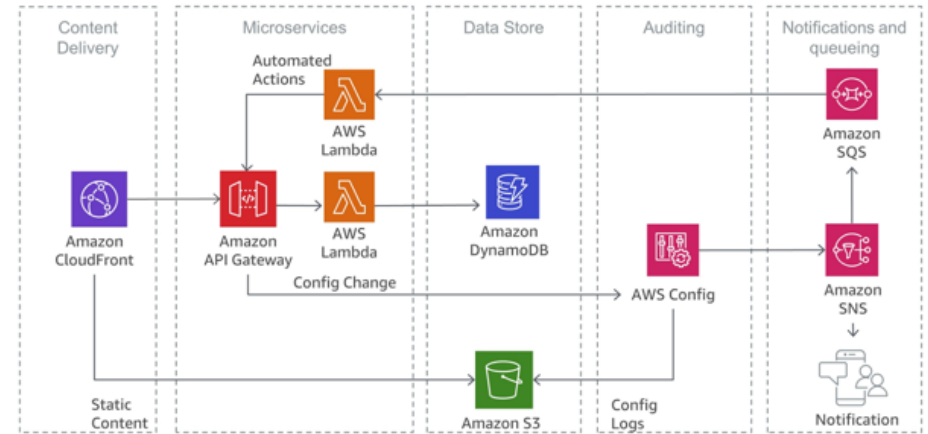
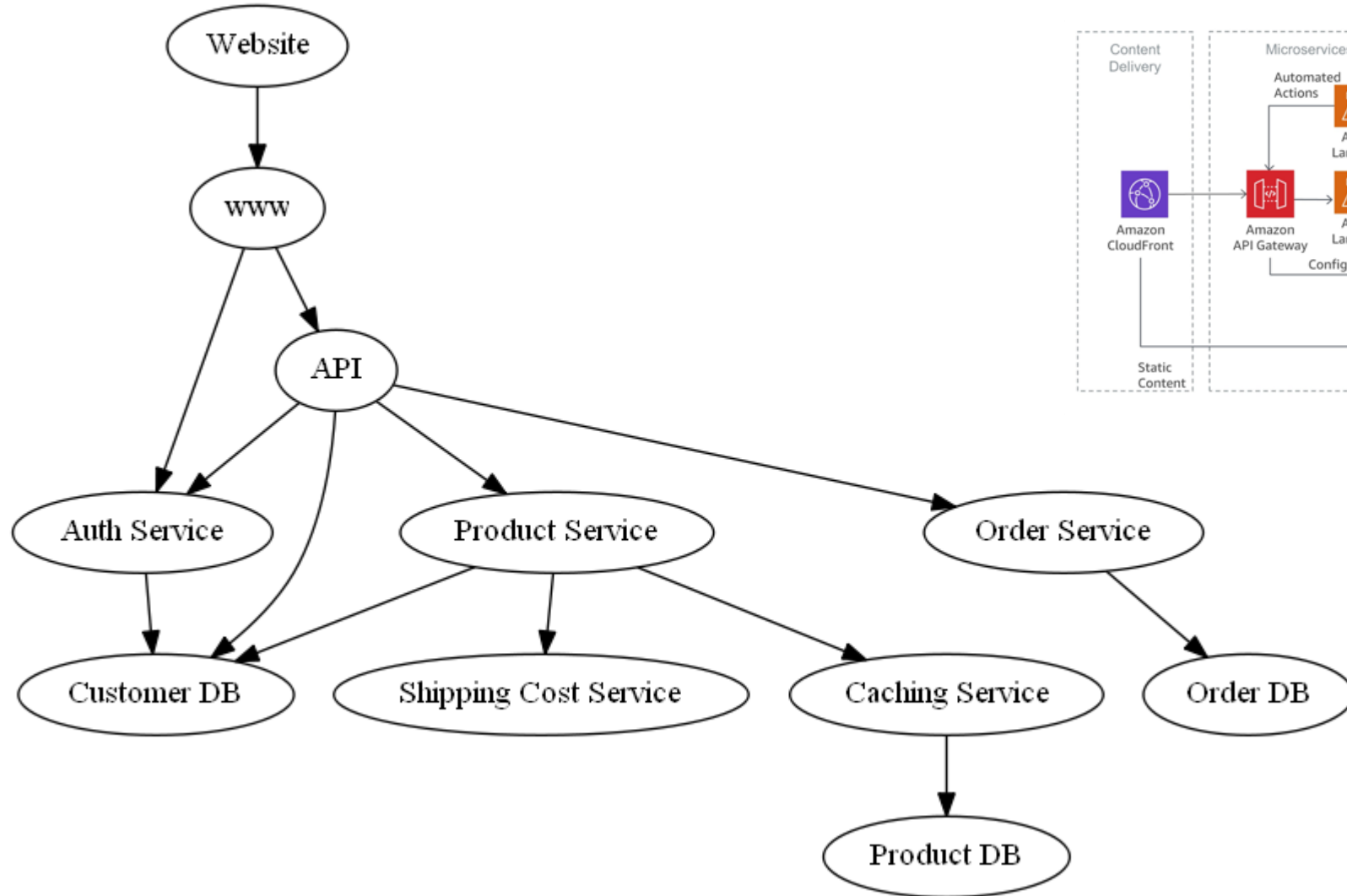
Use **domain knowledge** (Example 1)

- Estimating the effect of customer rewards program



How to obtain a causal graph?

Use **domain knowledge** (Example 2)



Section 3: Applications of causal ML (decision-making, root cause attribution, out-of-distribution generalization)

Decision-making: Given a target outcome, which action maximizes the outcome value?

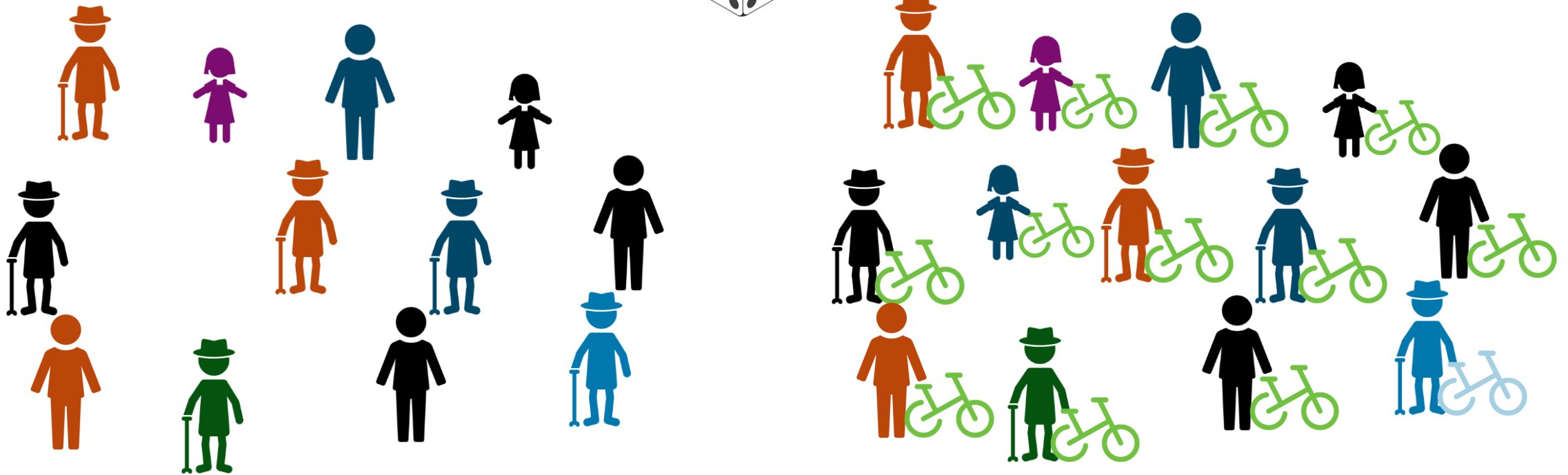
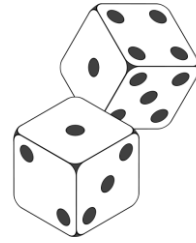
Frame as causal effect estimation problem

$$P(Y|do(A = a_1)), P(Y|do(A = a_2)), \dots$$

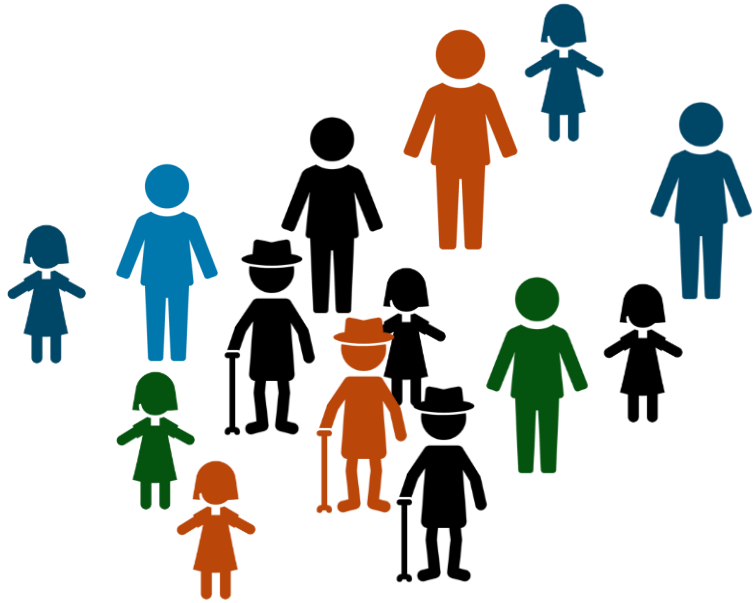
Rank the different causal effects

Choose the action with **highest causal effect on outcome.**

Randomized “A/B” test: A simple solution if you can intervene and create new data



But what to do if we **cannot intervene?**



People who do not cycle
have high cholesterol



People who cycle regularly
have low cholesterol

Simple Matching: Match data points with the same confounders and then compare their outcomes

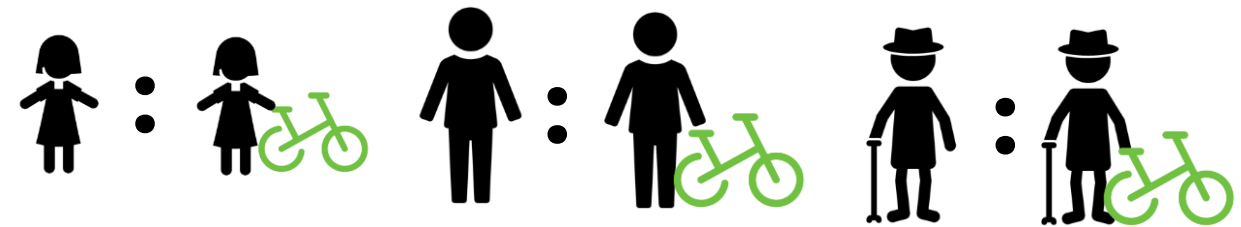
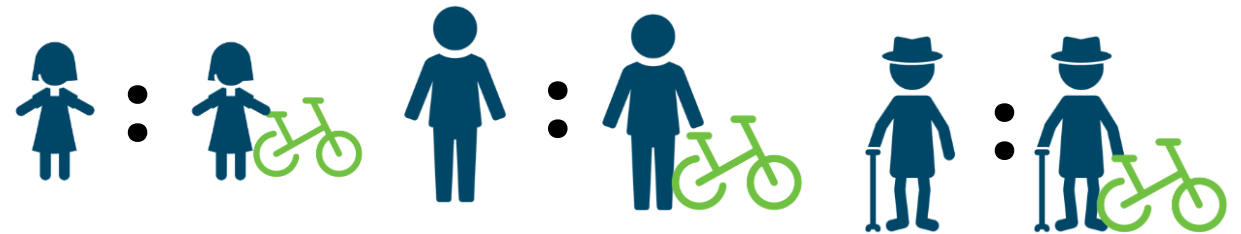
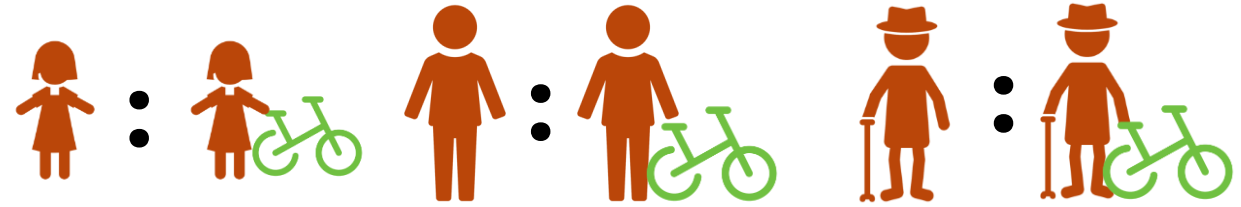
Identify pairs of treated (j) and untreated individuals (k) who are similar or identical to each other.

$$\text{Match} := \text{Distance}(W_j, W_k) < \epsilon$$

- Paired individuals have almost the same confounders.

Causal Effect =

$$\sum_{(j,k) \in \text{Match}} (y_j - y_k)$$



Challenges of building a good estimator

- **Variance:** If we have a stringent matching criterion, we may obtain very few matches and the estimate will be unreliable.
- **Bias:** If we relax the matching criterion, we obtain many more matches but now the estimate does not capture the target estimand.
- **Uneven treatment assignment:** If very few people have treatment, leads to both high bias and variance.

Need better methods to navigate the **bias-variance tradeoff**.

The intuition leads to a popular principle for estimating causal effect: **backdoor criterion**

Backdoor formula

$$p(Y|do(T)) = \sum_Z p(Y|T, Z)p(Z)$$

Where Z must be a valid adjustment set:

- The set of all parents of T
- Features identified via *backdoor criterion*
- Features identified via “towards necessity” criterion

Intuitions:

- The union of all features is *not* necessarily a valid adjustment set
- Why not always use parents? Sometimes parent features are unobserved

Voila! Effect inference problem reduced to estimating **conditional expectation**

For common identification strategies using adjustment sets,

$$E[Y|do(T = t), W = w] = E[Y|T = t, W = w]$$

assuming W is a valid adjustment set.

- For binary treatment,

$$\text{Causal Effect} = E[Y|T = 1, W = w] - E[Y|T = 0, W = w]$$

Goal: Estimating conditional probability $Y|T=t$ when all confounders W are kept constant.

Machine learning methods can help find a better match for each data point

Synthetic Control: If a good match does not exist for a data point, can we create it synthetically?

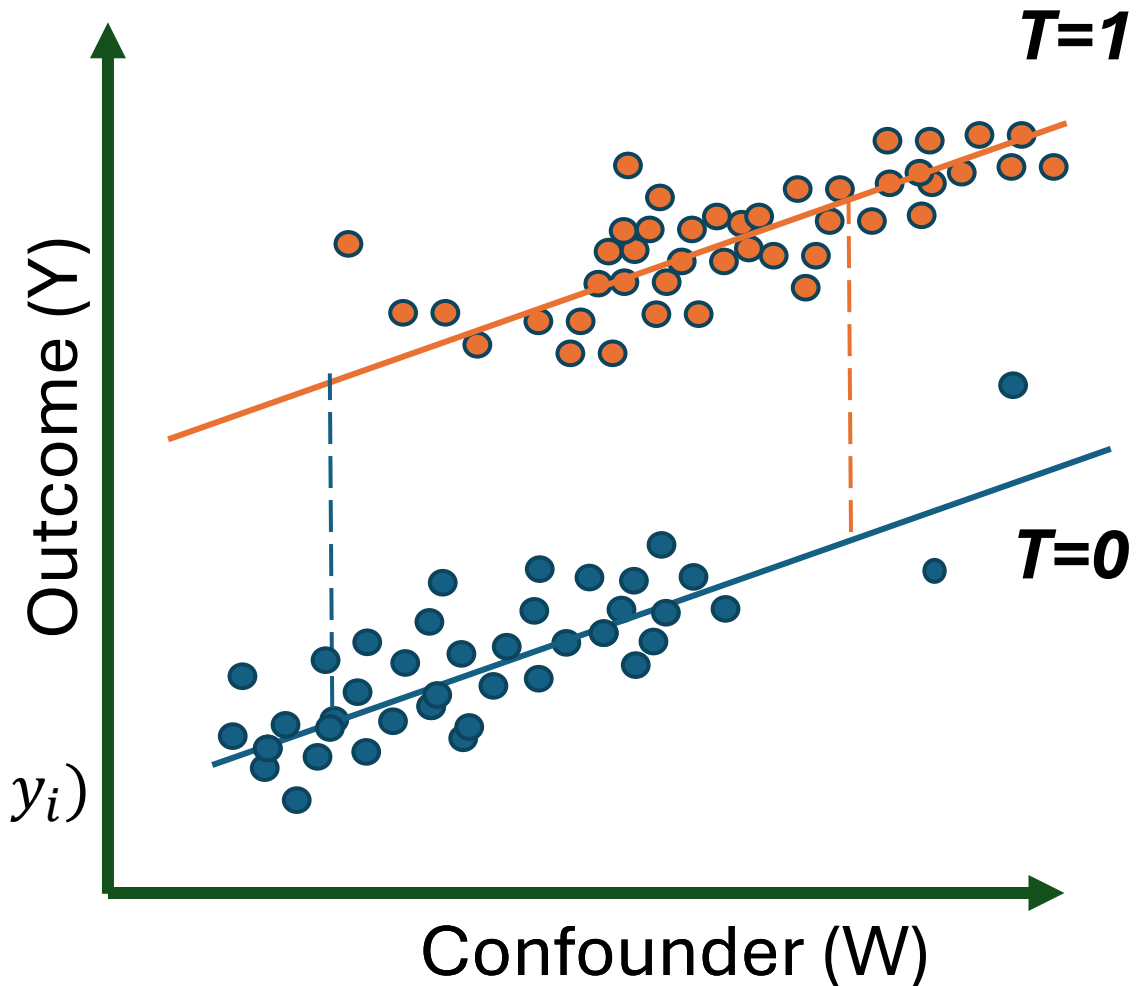
Learn $y = f_{t=0}(w)$,

$y = f_{t=1}(w)$

Assuming f approximates the true relationship between Y and W ,

Causal Effect =

$$\sum_i t_i(y_i - f_{t=0}(w_i)) + (1 - t_i)(f_{t=1}(w_i) - y_i)$$



A better solution: use **debiased ML** estimator

The standard predictor, $y = f(t, w) + \epsilon$
may not provide the right estimate for $\frac{\partial y}{\partial t}$.

Debiased-ML [Chernozhukov et al. 2016]:

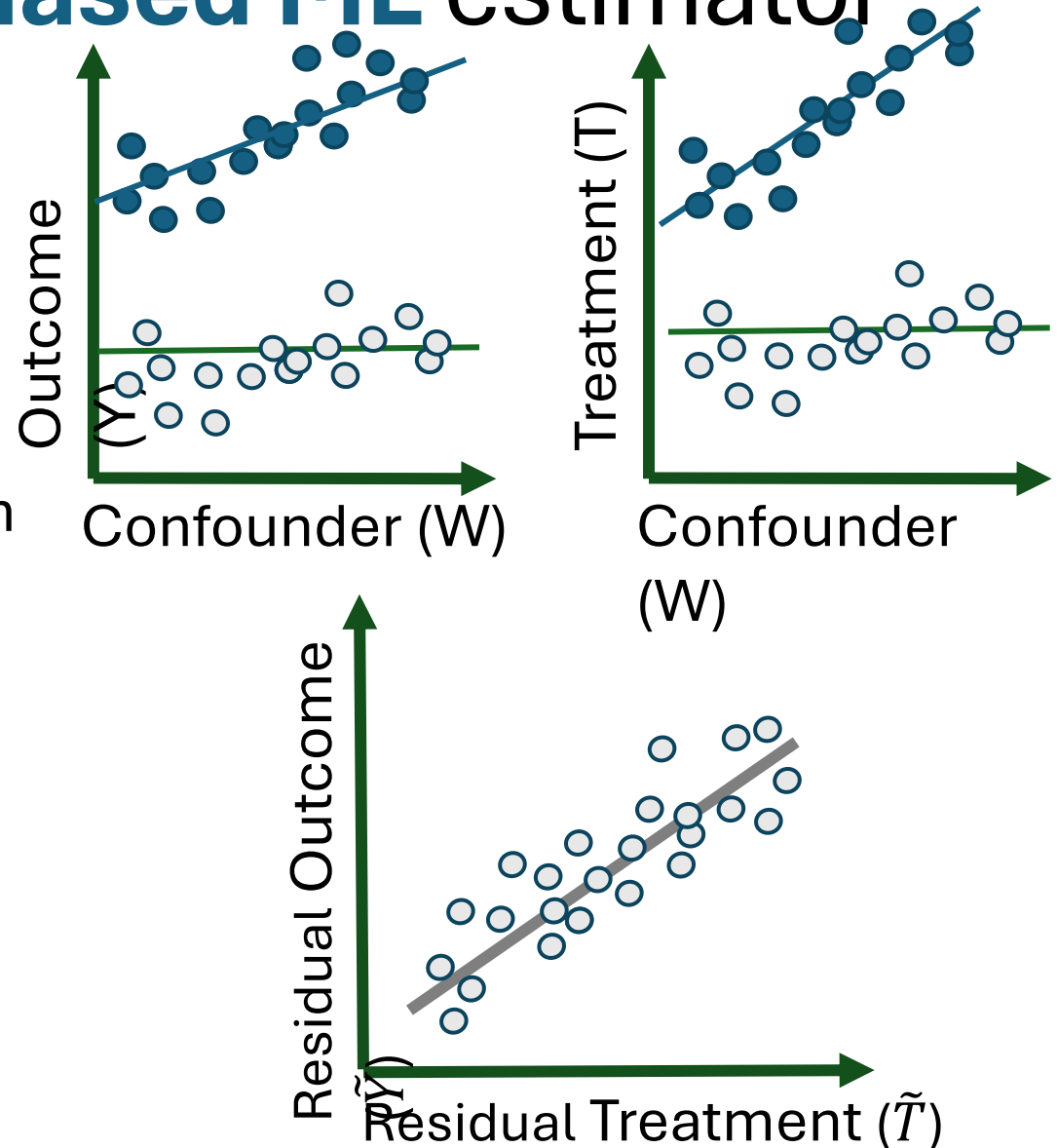
- **Stage 1:** Break down conditional estimation into two prediction sub-tasks.

$$\begin{aligned}\hat{y} &= g(w) + \tilde{y} \\ \hat{t} &= h(w) + \tilde{t}\end{aligned}$$

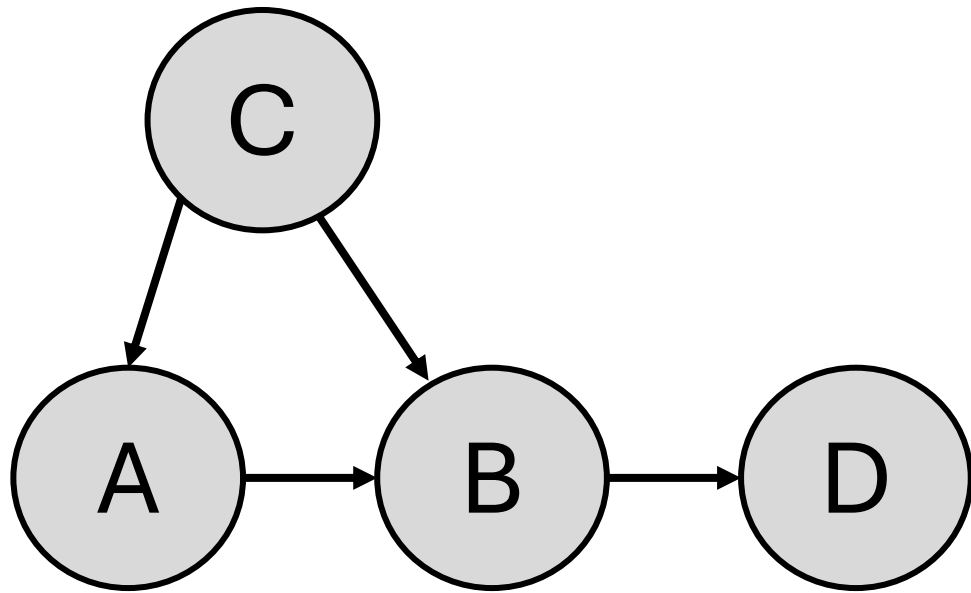
\tilde{y} and \tilde{t} refer to the unconfounded variation in Y and T respectively after conditioning on w .

- **Stage 2:** A final regression of \tilde{y} on \tilde{t} gives the causal effect.

$$\tilde{y} \sim \beta \tilde{t} + \epsilon$$



Second key application for causal ML: Root cause attribution



Causal effect can be identified with the just the graph structure.

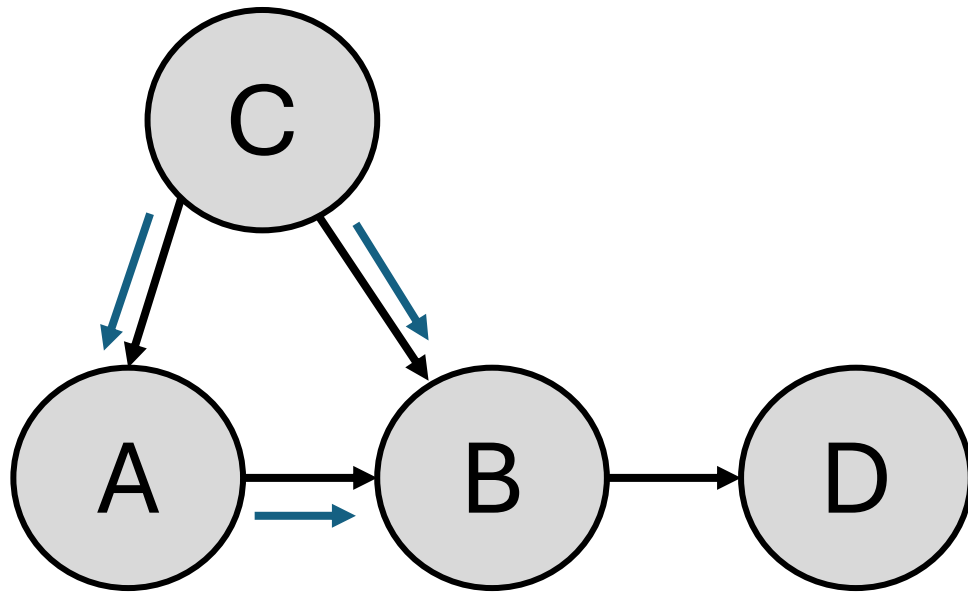
- Effect of A on B: $P(B|do(A)) = \sum_c P(B|A, C) P(C)$

For attribution, need to estimate the **counterfactual**.

Q: Given that $B = b$ and $C = c$, **how would B change if C was changed?**

$$P(B_{c'} | B = b, C = c, A = a, do(C = c'))$$

Second key application for causal ML: Root cause attribution



Q: Given that $B = b$ and $C = c$, **how would B change if C was changed?**

$$P(B_{c'} \mid B = b, C = c, A = a, do(C = c'))$$

If only do-intervention,

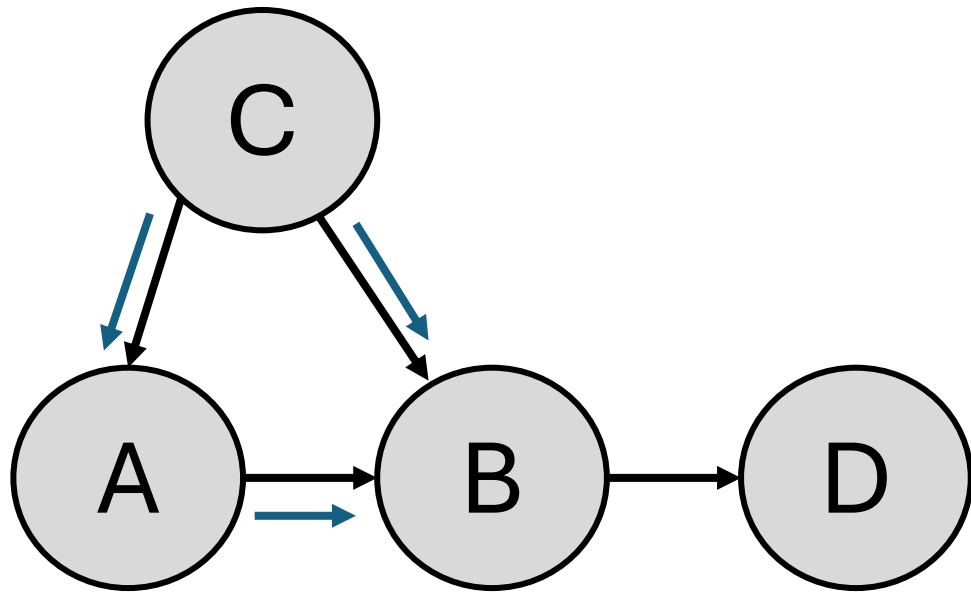
$$P(B \mid do(C = c')) = P(B \mid C)$$

But we also know that $B=b, C=c, A=a$ in observed data.

That constrains the value of B' .

\Rightarrow We need to know the **functional relationships** between A,B,C too.

The counterfactual generation algorithm



SCM: $A = g(C) + \epsilon_1$; $B = f(A, C) + \epsilon_2$

1. Abduction: Infer values of ϵ using observed data.

$$\epsilon_1^* = a - g(c); \epsilon_2^* = b - f(a, c)$$

2. Action: Set $C=c'$.

3. Prediction: Now propagate the change downstream through graph.

$$\begin{aligned} a' &= g(c') + \epsilon_1^* \\ b' &= f(a', c') + \epsilon_2^* \end{aligned}$$

Root cause attribution: Ranking over counterfactuals

- Using counterfactuals, we can now simulate the effect of different causes for an outcome.

$$P(Y_{X_1}), P(Y_{X_2}), P(Y_{X_3}), \dots$$

For attribution, we can rank the counterfactual effect of each cause.

Can also average wrt. the values of all other causes (e.g., using Shapley value)

Challenge: functional form is often unknown.

Practical usecase in attributing outcomes of a ML model.

Example: Consider a classification ML model over face images



Meryem Öztürk

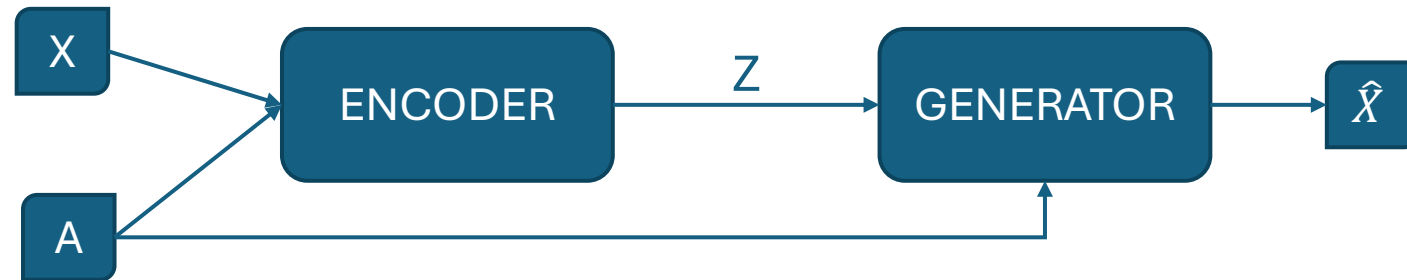
- Let's say there is a trained binary classification model using the image.
- It outputs class=1 for image 1. **Why?**
 - We may look at important features through ML explanation models like LIME, SHAP etc.
 - But those do not tell us how the model will behave if we change the input.

How to generate a counterfactual for a ML model

Tabular data: Simply change the input name.

Image data: Need an encoder-generator architecture.

$$z = E(x, a); \quad \text{Counterfactual}_{(A=a')} = G(z, a')$$



Train using Adversarially Learnt Inference [Dumoulin et al. 2016]

$$\min_{G,E} \max_D V(G, E, D) = E[\log(D(x, E(x, a), a))] + E[1 - D(G(z, a), z, a)]$$

Evaluating a ML classifier on a Face dataset

CelebA dataset (Photos with 40 attributes like hair color, skin color, etc.)

Generate counterfactuals for each image.

Given a CNN classifier for one of the attributes (“attractiveness”), trained using standard loss minimization.

- **Explain:** Which attributes are considered important for prediction?
- **Fairness:** Is it fair wrt. certain attributes (*pale skin* attribute)?



Reconstructed

BlackHair

BlackHair,
PaleSkin

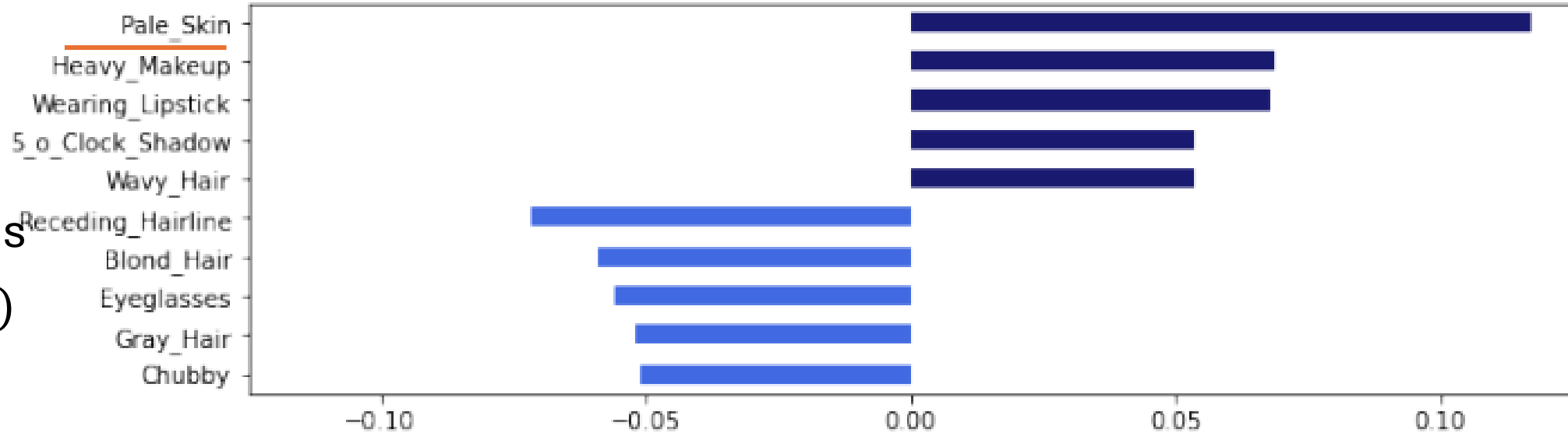
BlondeHair

BlondeHair,
PaleSkin

Explain:

Feature importance scores

$$f(X_{A_i=a'}) - f(X)$$



Fairness:

Bias wrt. different features

$$P(f(X_{A_i=a'}) = 1, f(X) = 0) - P(f(X_{A_i=a'}) = 0, f(X) = 1)$$

	$p(a_r \neq a_c)$	$p(0 \rightarrow 1)$	bias
Horizontal_Flip	0.071	0.496	0.000
Brightness	0.137	0.619	0.033
black_h	0.067	0.838	0.045
black_h, pale	0.177	0.996	0.175
blond_h	0.090	0.115	- 0.069
blond_h, pale	0.095	0.773	0.052
brown_h	0.057	0.877	0.043
brown_h, pale	0.165	0.999	0.165
bangs	0.084	0.845	0.058

Third key application for causal ML:

Out-of-distribution generalization

Domain generalization

Multiple domains: Assume access to data from multiple distributions

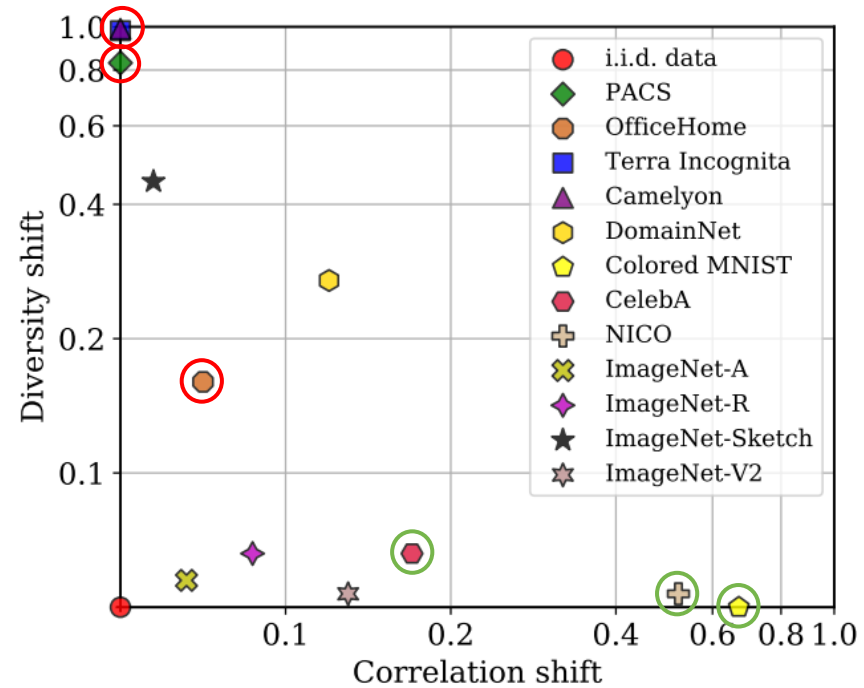
- Learn invariant patterns across the different sources
 - Invariant Risk Minimization (Arjovsky et al., 2019)
 - (Krueger et al. 2020, Ganin et al. 2016, Gulrajani & Lopez-Paz 2021, Nam et al. 2021)

Group generalization

Single domain: Assume access to group attributes for each input

- Equalize accuracy across groups/maximize worst-group accuracy
 - Group-DRO (Sagawa et al., 2020), (Ahmed et al. 2021)

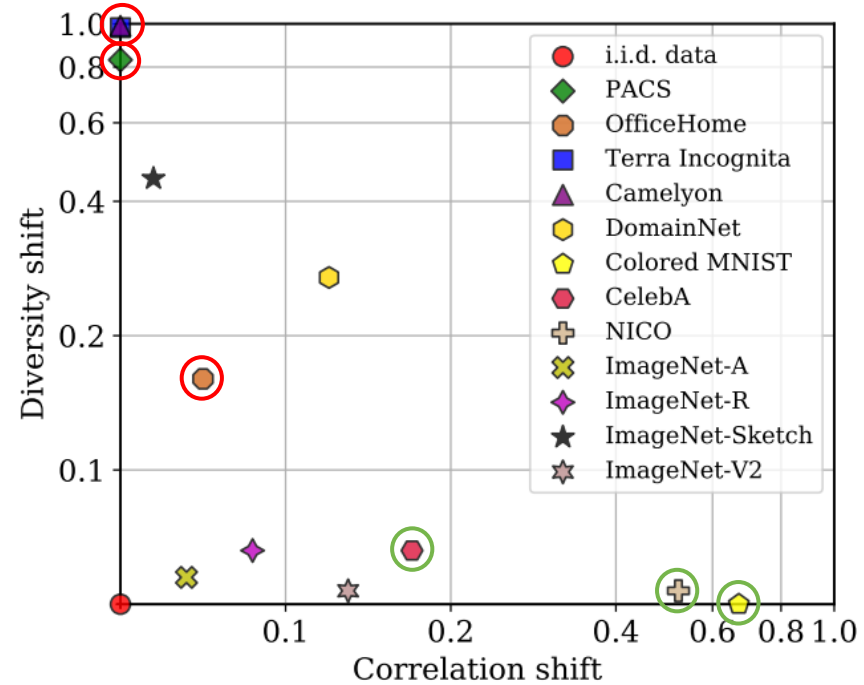
Sobering state of SoTA algorithms



Sobering state of SoTA algorithms

	Train		Test
	15°	60°	90°
Y=0			
Y=1			

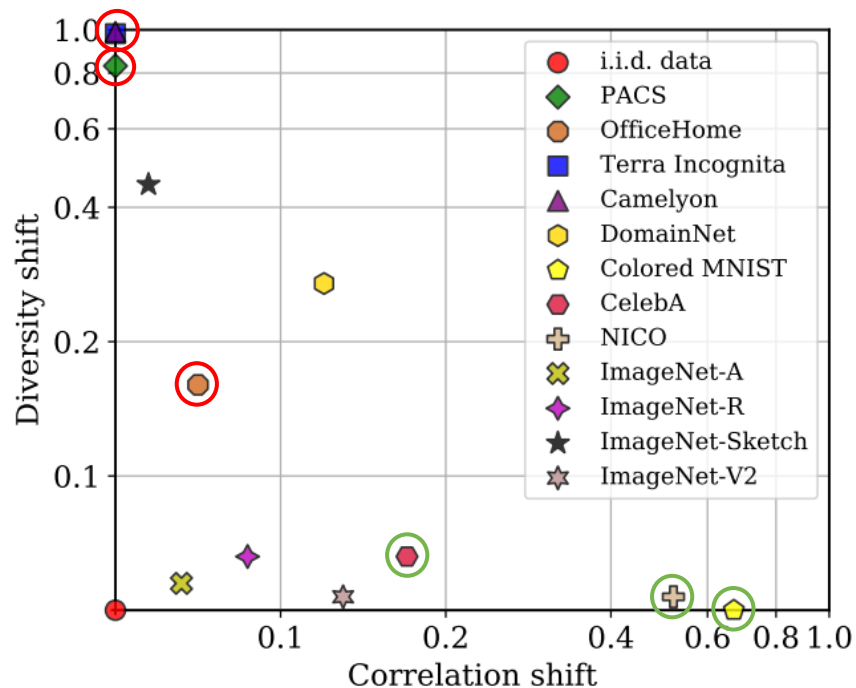
Rotated MNIST



Sobering state of SoTA algorithms

	Train		Test
	15°	60°	90°
Y=0			
Y=1			

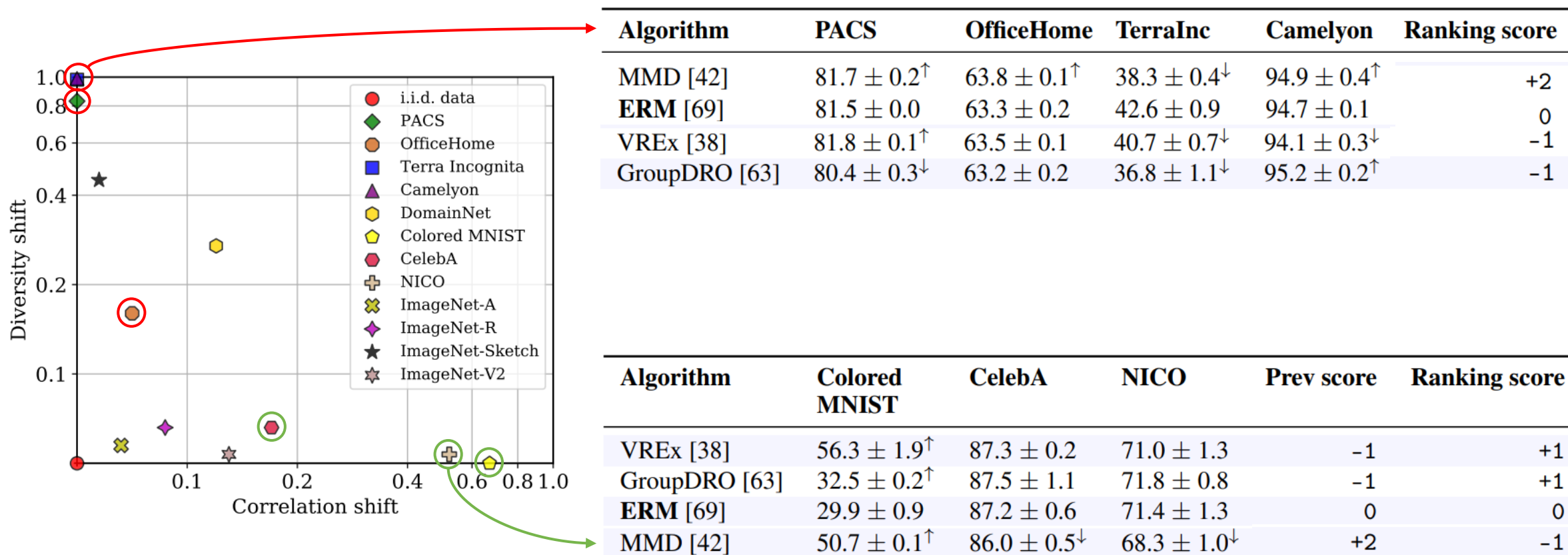
Rotated MNIST



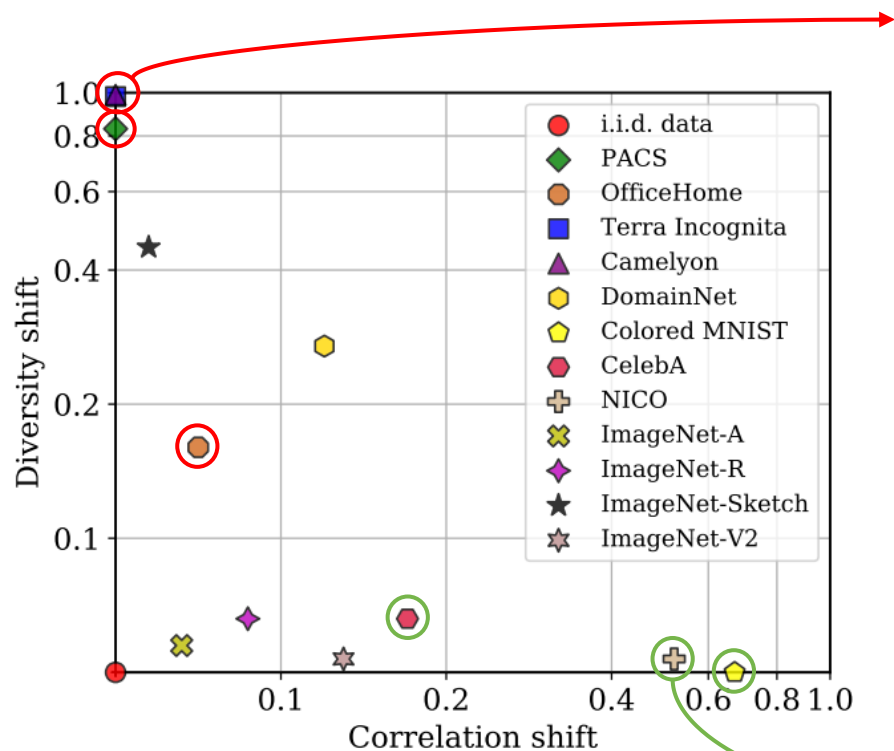
	Train		Test
	0.9	0.8	0.1
Y=0			
Y=1			

Colored MNIST

Sobering state of SoTA algorithms



Sobering state of SoTA algorithms



Algorithm	PACS	OfficeHome	TerraInc	Camelyon	Ranking score
MMD [42]	$81.7 \pm 0.2^\uparrow$	$63.8 \pm 0.1^\uparrow$	$38.3 \pm 0.4^\downarrow$	$94.9 \pm 0.4^\uparrow$	+2
ERM [69]	81.5 ± 0.0	63.3 ± 0.2	42.6 ± 0.9	94.7 ± 0.1	0
VREx [38]	$81.8 \pm 0.1^\uparrow$	63.5 ± 0.1	$40.7 \pm 0.7^\downarrow$	$94.1 \pm 0.3^\downarrow$	-1
GroupDRO [63]	$80.4 \pm 0.3^\downarrow$	63.2 ± 0.2	$36.8 \pm 1.1^\downarrow$	$95.2 \pm 0.2^\uparrow$	-1

No method can surpass ERM on all kinds of shifts!

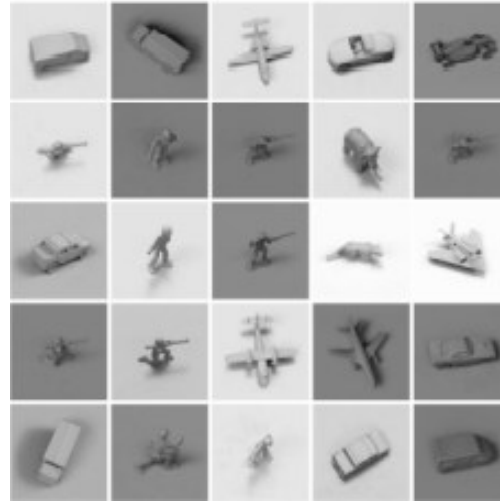
Algorithm	Colored MNIST	CelebA	NICO	Prev score	Ranking score
VREx [38]	$56.3 \pm 1.9^\uparrow$	87.3 ± 0.2	71.0 ± 1.3	-1	+1
GroupDRO [63]	$32.5 \pm 0.2^\uparrow$	87.5 ± 1.1	71.8 ± 0.8	-1	+1
ERM [69]	29.9 ± 0.9	87.2 ± 0.6	71.4 ± 1.3	0	0
MMD [42]	$50.7 \pm 0.1^\uparrow$	$86.0 \pm 0.5^\downarrow$	$68.3 \pm 1.0^\downarrow$	+2	-1

Sobering state of SoTA algorithms



IID

[Correlation Shift]



Spurious correlation
b/w category and lighting






[Diversity Shift]



Unseen data shift
unseen azimuth values

Best methods are not consistent over different datasets and shifts

What if different distribution shifts co-exist?

	Train			Test	
Satellite Image (x)					
Year / Region (d)	2002 / Americas	2009 / Africa	2012 / Europe	2016 / Americas	2017 / Africa
Building / Land Type (y)	shopping mall	multi-unit residential	road bridge	recreational facility	educational institution

What if different distribution shifts co-exist?

Rotation		Train		Test
		15°	60°	90°
	Y=0			
	Y=1			

+

Color		Train		Test
		0.9	0.8	0.1
	Y=0			
	Y=1			

Col+Rot		(0.9,15°)	(0.8,60°)	(0.1,90°)
	Y=0			
	Y=1			

Accuracy decreases further for all algorithms.

Algorithm	Color	Rotation	Col+Rot
ERM	30.9 ± 1.6	61.9 ± 0.5	25.2 ± 1.3
IRM	50.0 ± 0.1	61.2 ± 0.3	39.6 ± 6.7
MMD	29.7 ± 1.8	62.2 ± 0.5	24.1 ± 0.6
C-MMD	29.4 ± 0.2	62.3 ± 0.4	32.2 ± 7.0



I. Causal reasoning can explain this failure

[single shift] Explain results from causal perspective

- Different distribution shifts arise due to differences in data-generating process (DGP)
 - Leading to different independence constraints
- No single independence constraint can work for all shifts

II. Causal reasoning can provide a better algorithm

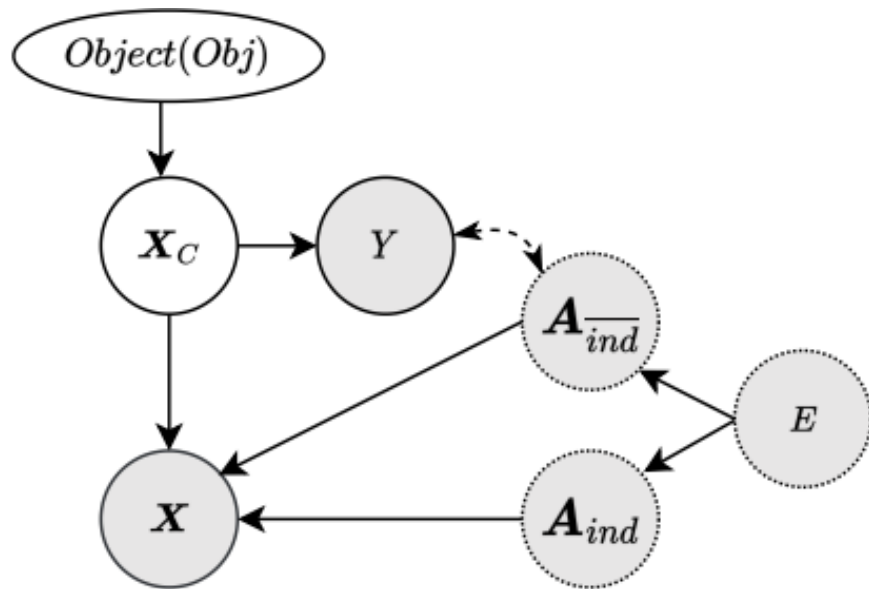
[single shift] Explain results from causal perspective

- Different distribution shifts arise due to differences in data-generating process (DGP)
 - Leading to different independence constraints
- No single independence constraint can work for all shifts

[multi-shift] Can we develop an algorithm that generalizes to individual as well as multi-attribute shifts?

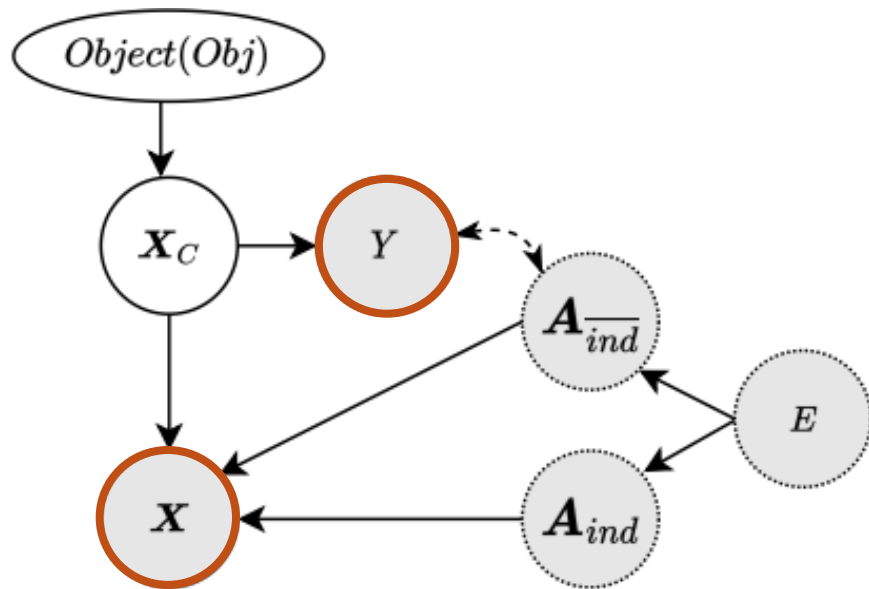
- We propose *Causally Adaptive Constraint Minimization (CACM)* to model the causal relationships in DGP

Representation of shifts using causal graph



Causal DAG to specify multi-attribute shifts

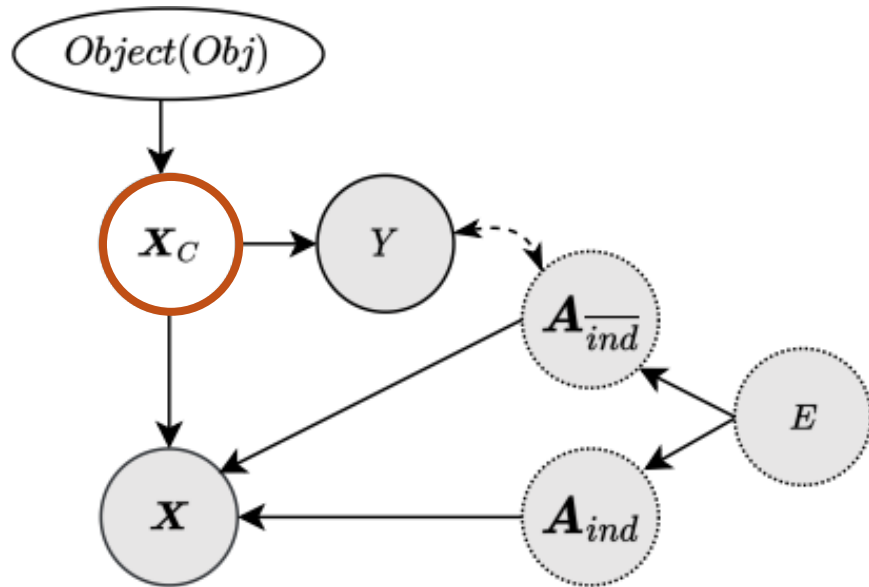
Representation of shifts using causal graph



Observed variables X, Y

Causal DAG to specify multi-attribute shifts

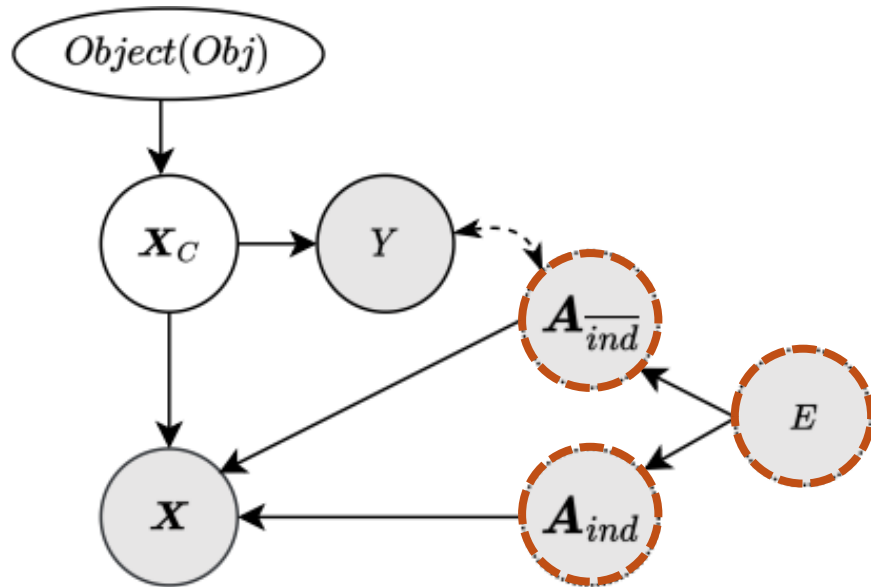
Representation of shifts using causal graph



Observed variables X, Y
Causal features X_c

Causal DAG to specify multi-attribute shifts

Representation of shifts using causal graph



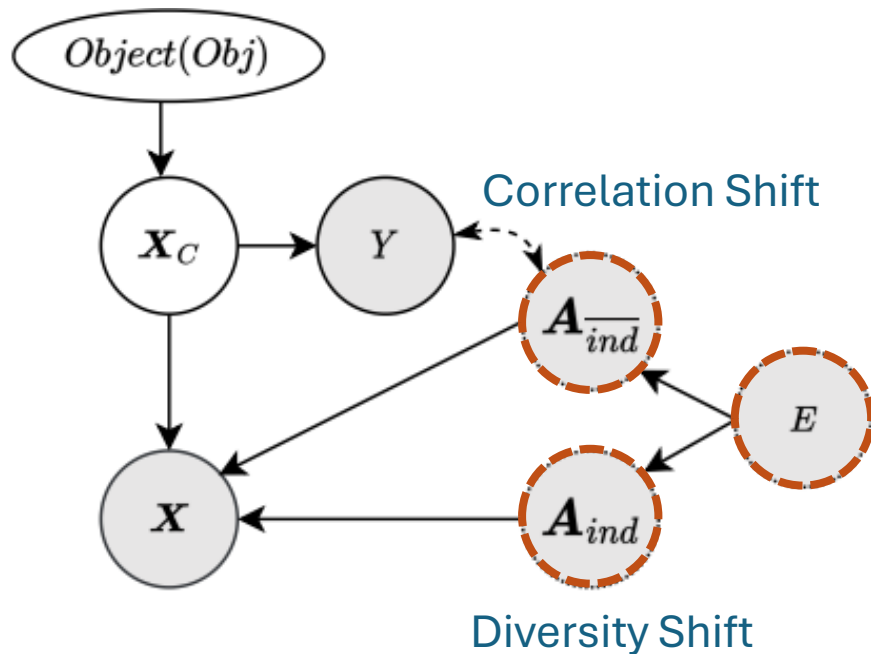
Observed variables X, Y

Causal features X_c

Attributes $A_{ind}, A_{\overline{ind}}, E$ st $A_{ind} \cup A_{\overline{ind}} \cup \{E\} = A$

Causal DAG to specify multi-attribute shifts

Representation of shifts using causal graph



Observed variables X, Y

Causal features X_c

Attributes $A_{ind}, A_{ind}^{\overline{}}, E$ st $A_{ind} \cup A_{ind}^{\overline{}} \cup \{E\} = A$

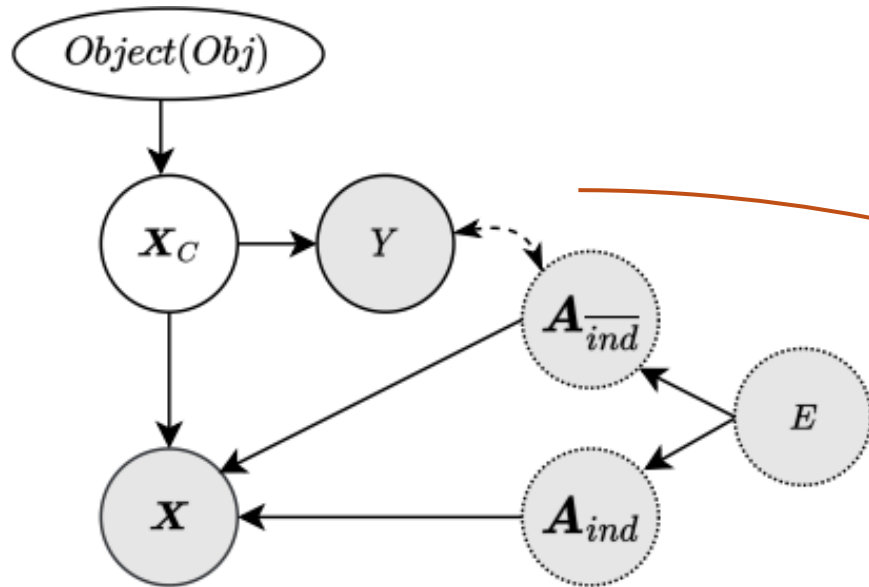
independent
of label

correlated
with label

domain
attribute

Causal DAG to specify multi-attribute shifts

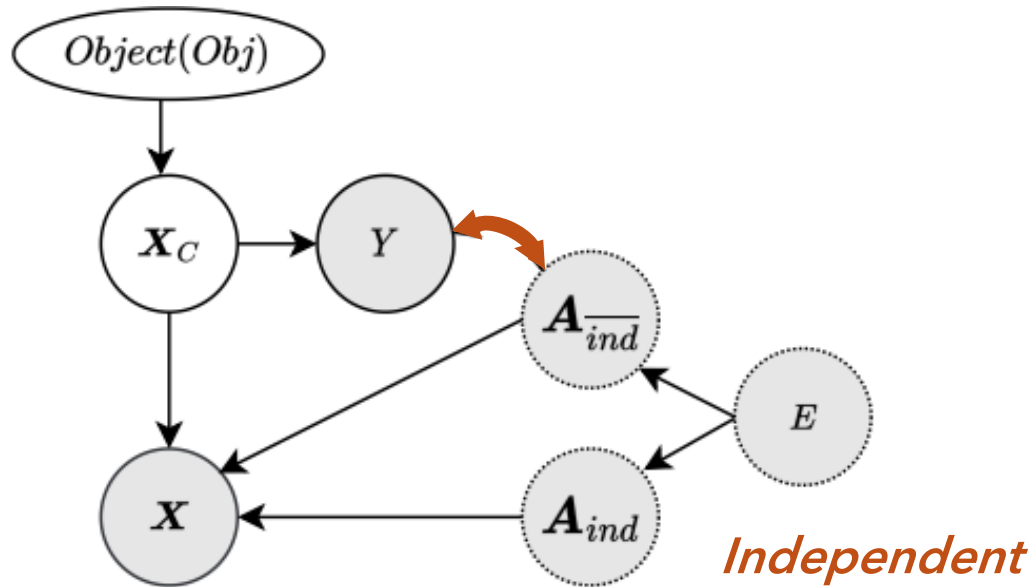
Representation of shifts using causal graph



Causal DAG to specify multi-attribute shifts

Different $Y - A_{\overline{ind}}$ relationships

Representation of shifts using causal graph

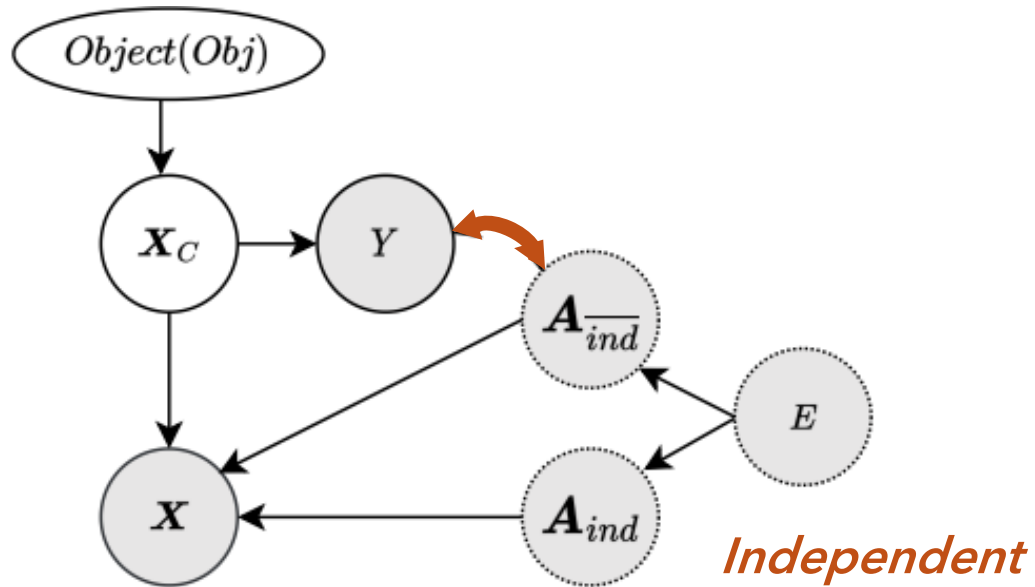


Causal DAG to specify multi-attribute shifts

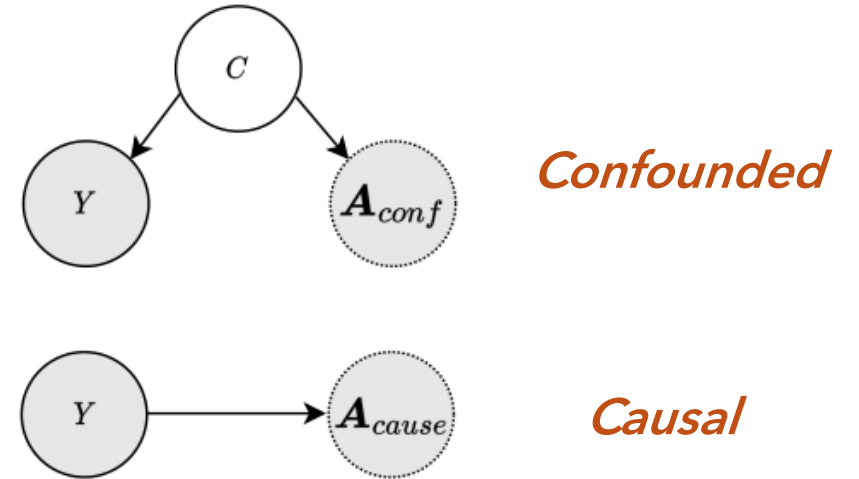


Different $Y - A_{\overline{ind}}$ relationships

Representation of shifts using causal graph

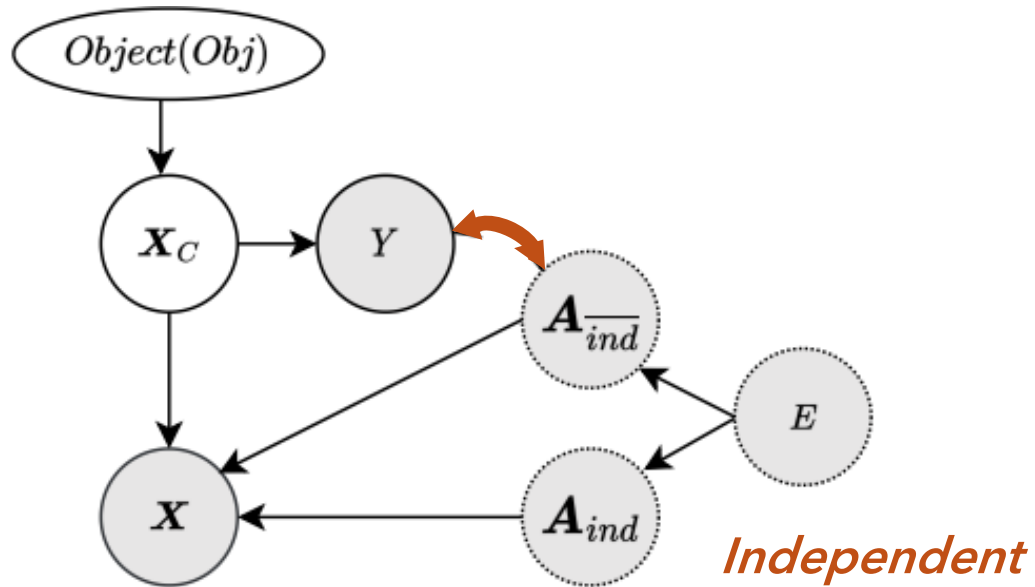


Causal DAG to specify multi-attribute shifts

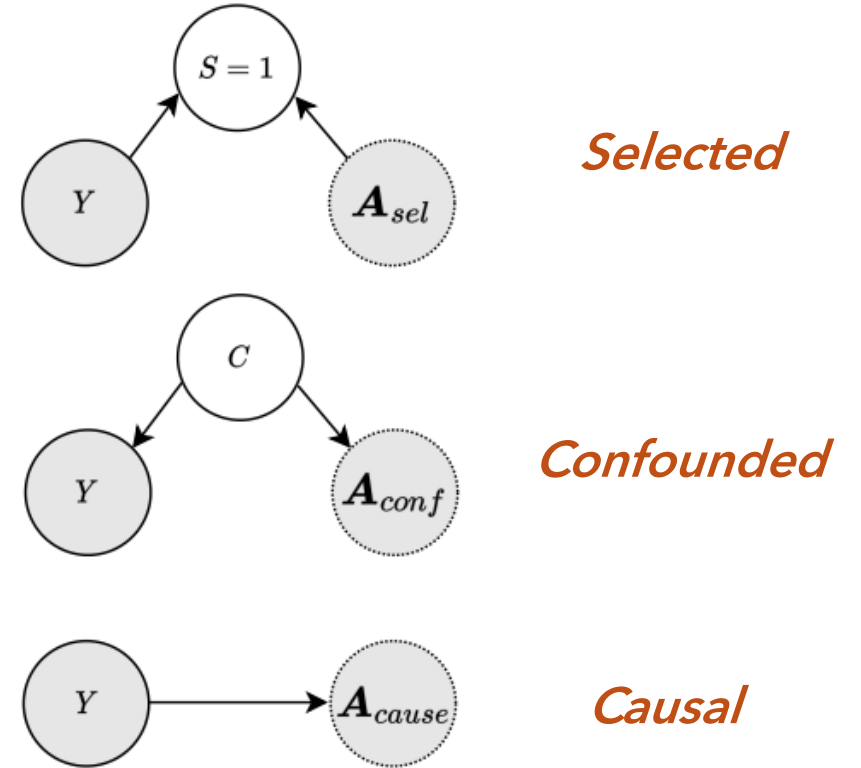


Different $Y - A_{\overline{ind}}$ relationships

Representation of shifts using causal graph



Causal DAG to specify multi-attribute shifts



Different $Y - A_{\overline{ind}}$ relationships

Back to the MNIST example

Rotation		Train		Test
		15°	60°	90°
	Y=0			
Y=1				

A_{ind}

+

Color		Train		Test
		0.9	0.8	0.1
	Y=0			
Y=1				

A_{cause}

(A_{ind})

Col+Rot

	(0.9, 15°)	(0.8, 60°)	(0.1, 90°)
Y=0			
Y=1			

Causal + Independent

$A_{cause} \cup A_{ind}$

Generalization to multi-attribute shifts

Algorithm	Color	Rotation	Col+Rot
ERM	30.9 ± 1.6	61.9 ± 0.5	25.2 ± 1.3
IRM	50.0 ± 0.1	61.2 ± 0.3	39.6 ± 6.7
MMD	29.7 ± 1.8	62.2 ± 0.5	24.1 ± 0.6
C-MMD	29.4 ± 0.2	62.3 ± 0.4	32.2 ± 7.0
<i>CACM</i>	70.4 ± 0.5	62.4 ± 0.4	54.1 ± 0.3

CACM outperforms on individual as well as combination of shifts

The *CACM* Approach

Identifying the correct regularizer under multi-attribute shifts

The *CACM* Approach

Identifying the correct regularizer under multi-attribute shifts

- I. Derive correct independence constraints for \mathbf{X}_c based on causal graph
- II. Apply the constraints as regularizer to standard ERM loss.

Step I: Deriving independence constraints

Predictor $g(\mathbf{x}) = g_1(\phi(\mathbf{x}))$

Representation ϕ should follow same conditional independence constraints as \mathbf{X}_c

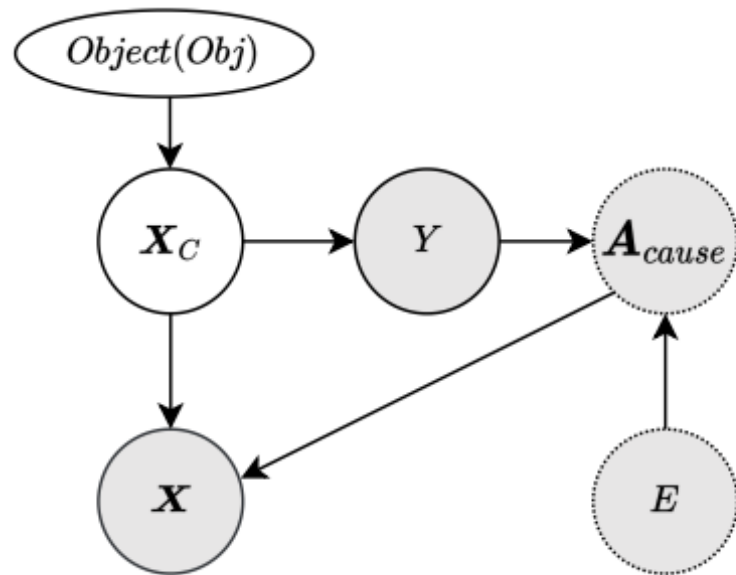
Step I: Deriving independence constraints

Predictor $g(\mathbf{x}) = g_1(\phi(\mathbf{x}))$

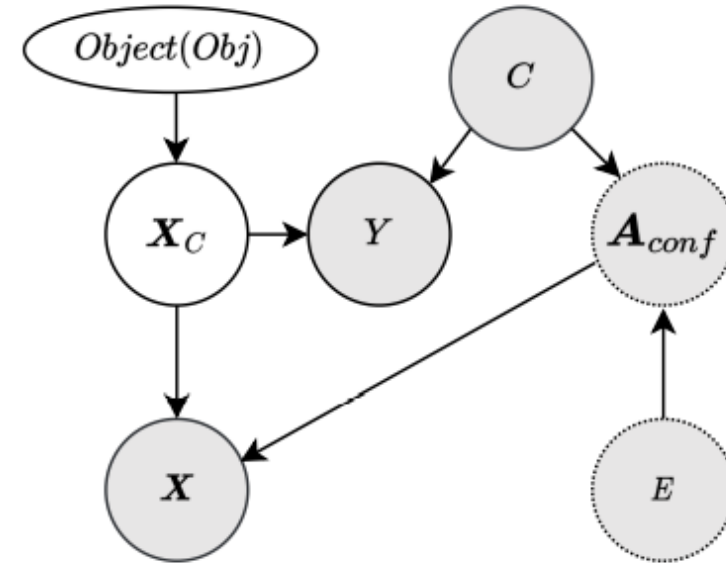
Representation ϕ should follow same conditional independence constraints as \mathbf{X}_c

Proposition 3.1. Given a dataset $(\mathbf{x}_i, \mathbf{a}_i, y_i)_{i=1}^n$ and a causal DAG over $\langle \mathbf{X}_c, \mathbf{X}, \mathbf{A}, Y \rangle$ such that \mathbf{X}_c is the only variable (or set of variables) that causes Y and is not independent of \mathbf{X} , then the conditional independence constraints satisfied by \mathbf{X}_c are necessary for a risk-invariant predictor.

Step I: Deriving independence constraints



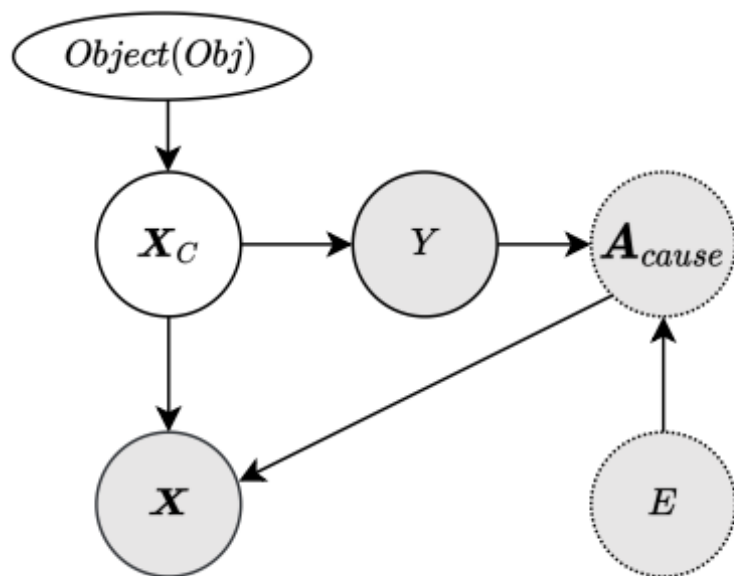
Causal



Confounded

Different $Y - A_{ind}$ relationships lead to different constraints

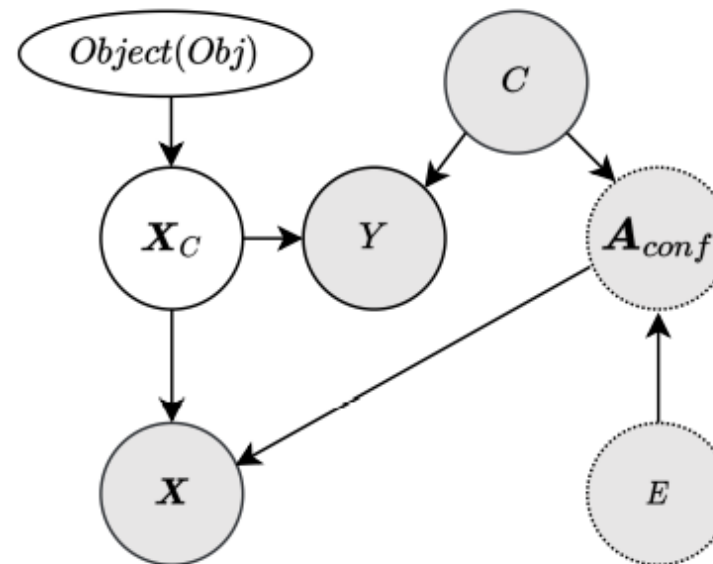
Step I: Deriving independence constraints



Causal

$$X_c \perp\!\!\!\perp A_{cause} \mid Y, E \quad \checkmark$$

$$X_c \perp\!\!\!\perp A_{cause} \mid E \quad \times$$



Confounded

$$X_c \perp\!\!\!\perp A_{conf} \mid Y, E \quad \times$$

$$X_c \perp\!\!\!\perp A_{conf} \mid E \quad \checkmark$$

Step II: Applying regularization penalty

Constraint: $\mathbf{X}_c \perp\!\!\!\perp \mathbf{A}_{cause} \mid Y, E$ [*Causal* shift]

$$RegPenalty_{\mathbf{A}_{cause}} = \sum_{|E|} \sum_{y \in Y} \sum_{i=1}^{|\mathbf{A}_{cause}|} \sum_{j>i} \text{MMD} \left(P(g_1(\phi(\mathbf{x})) \mid a_{i,cause}, y), P(g_1(\phi(\mathbf{x})) \mid a_{j,cause}, y) \right)$$

$$\mathbf{g}_1, \phi = \operatorname{argmin}_{\mathbf{g}_1, \phi} L(g_1(\phi(\mathbf{x})), y) + \lambda^*(RegPenalty_{\mathbf{A}_{cause}})$$

Summary of Session 1

- Causal ML is important whenever we have decision-making or attribution tasks, or want generalizability of predictive model beyond the training distribution.
- Causal graph is the most important assumption.
 - “No causes in, no causes out” – Judea Pearl
- The goal is to develop methods that use the least amount of assumptions.
 - E.g., debiased ML for effect estimation
 - Simple, high-level causal graph for images